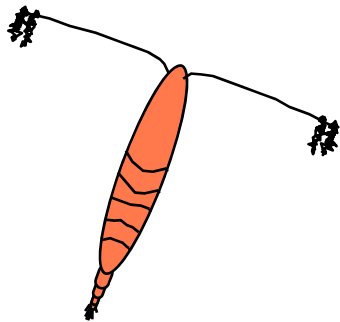
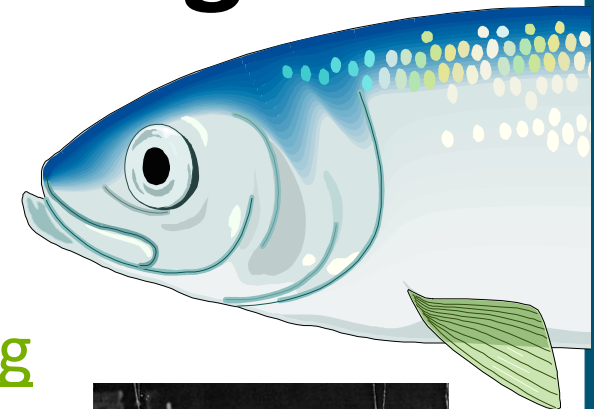


# Optimality models of behaviour and life strategies

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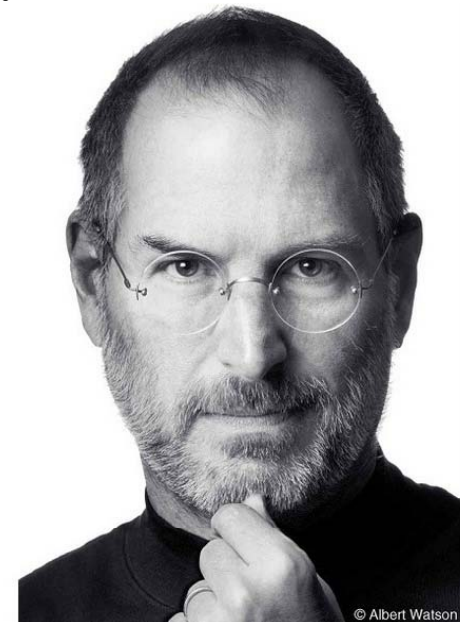
[www.bio.uib.no/te](http://www.bio.uib.no/te)



# Computers..

**"So we used them in our work, but...much more importantly... it had nothing to do with using them for anything practical. It had to do with...to be a mirror of your thought process, to actually learn how to think.. I think everybody in this country should learn how to program a computer, should learn a computer language, because it teaches you how to think."**

**- Steve Jobs, 1995**



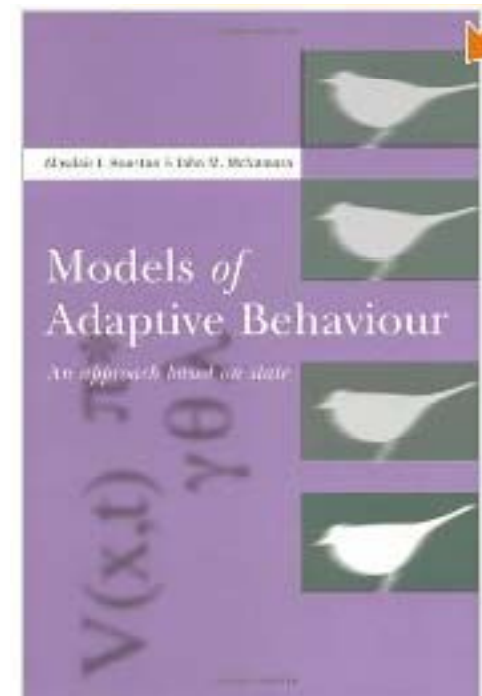
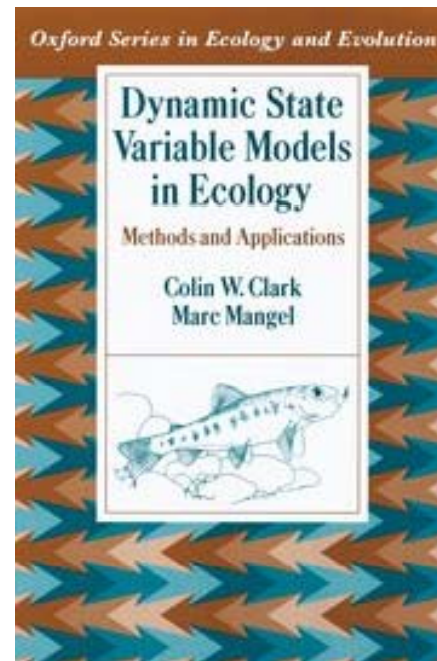
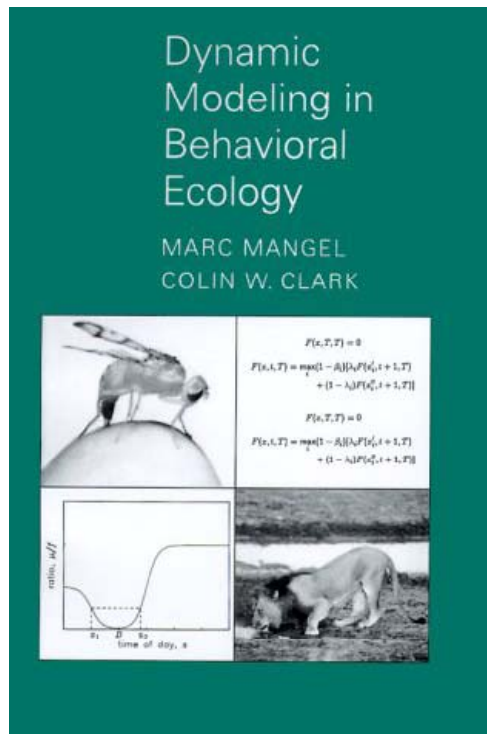
© Albert Watson

# Optimality theory

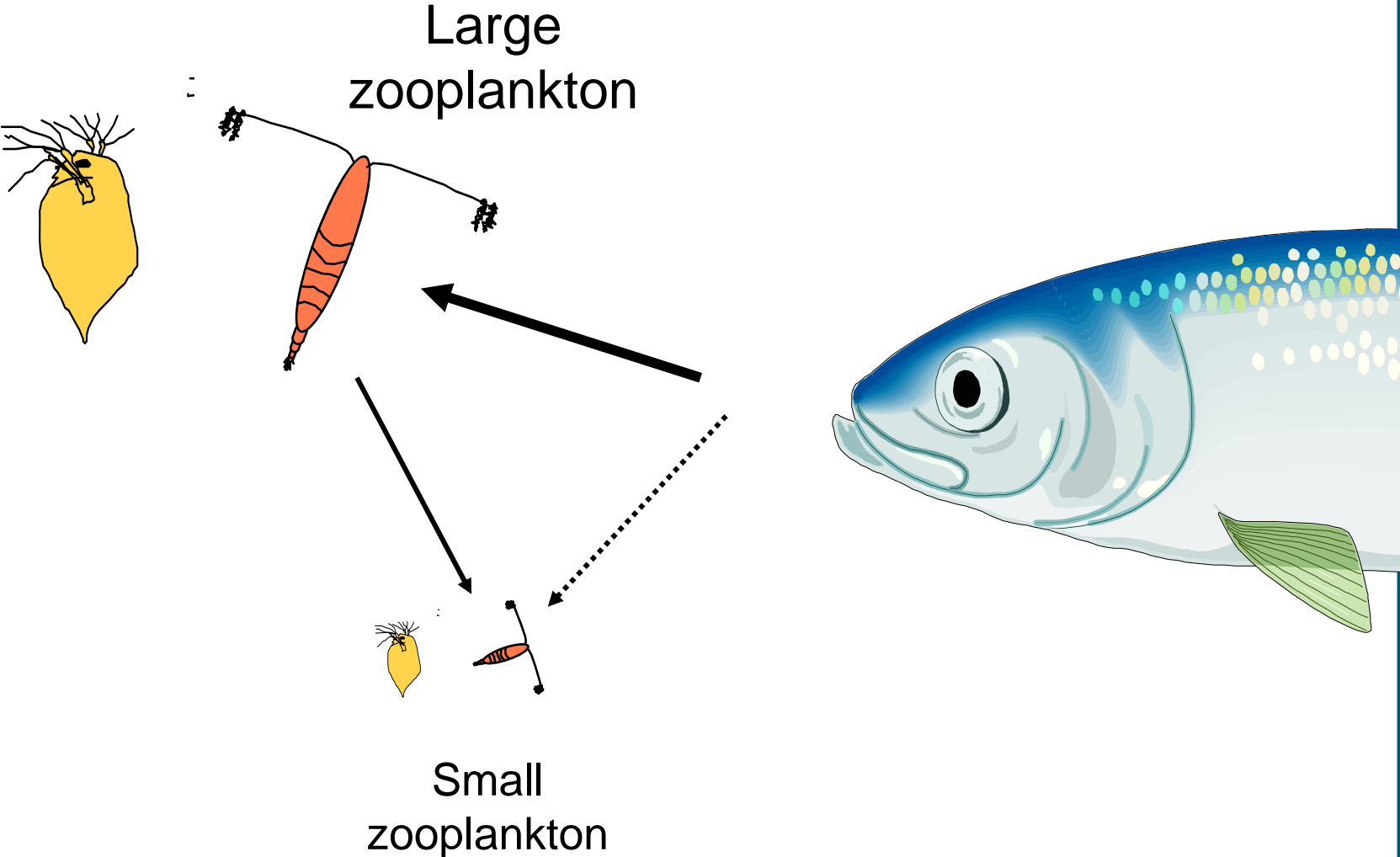
- **Strategy or decision** – which traits are optimized
- **Currency** – what is maximized, or ‘fitness’ measure
- **Constraints** – what are the limits and trade-offs
- **States** – what are the relevant attributes

# Dynamic programming

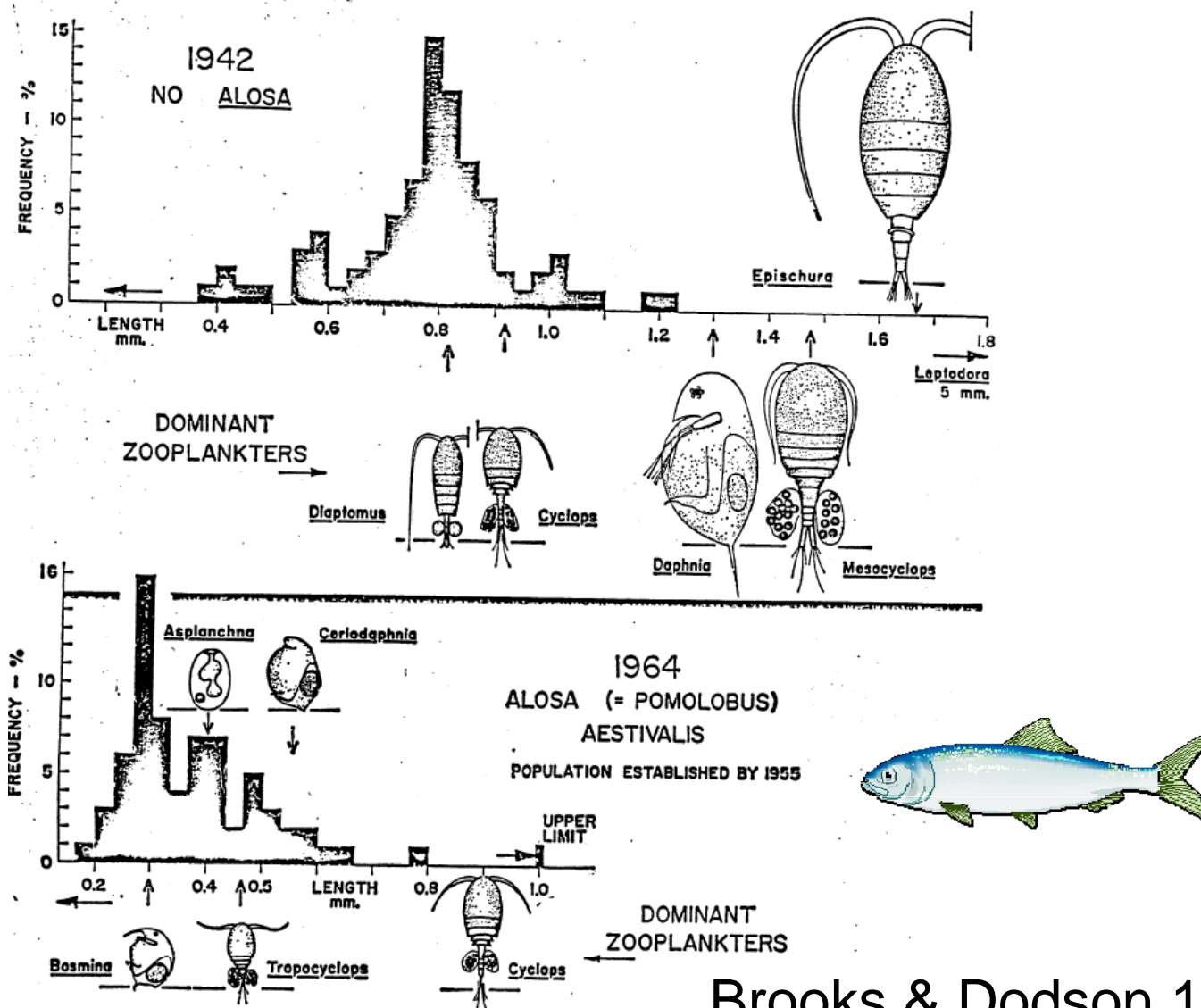
## State-variable models



# Fish-plankton interaction primer..



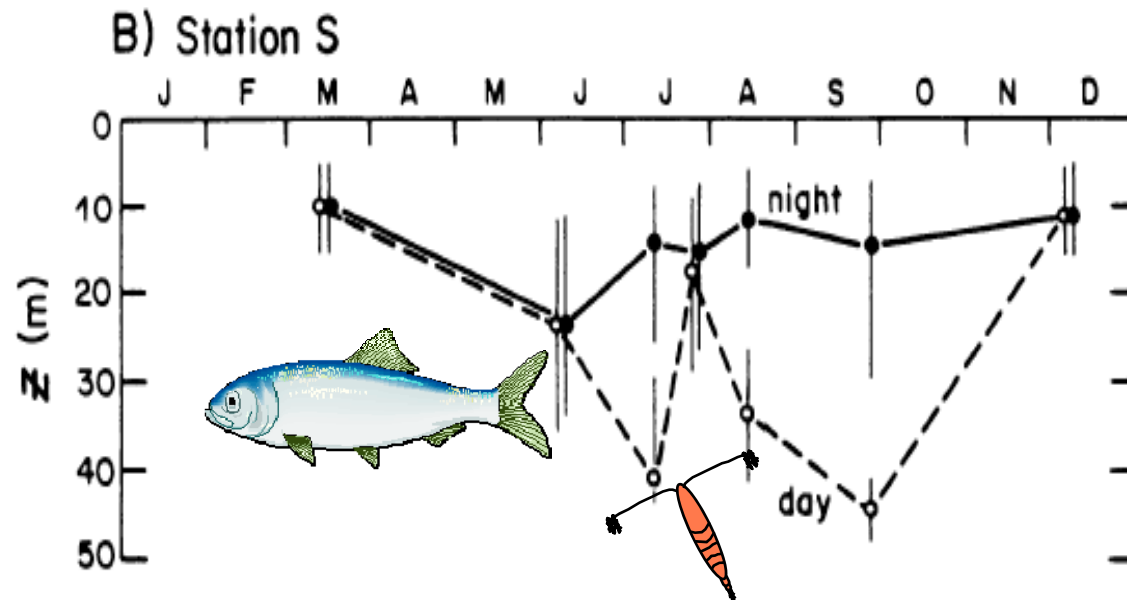
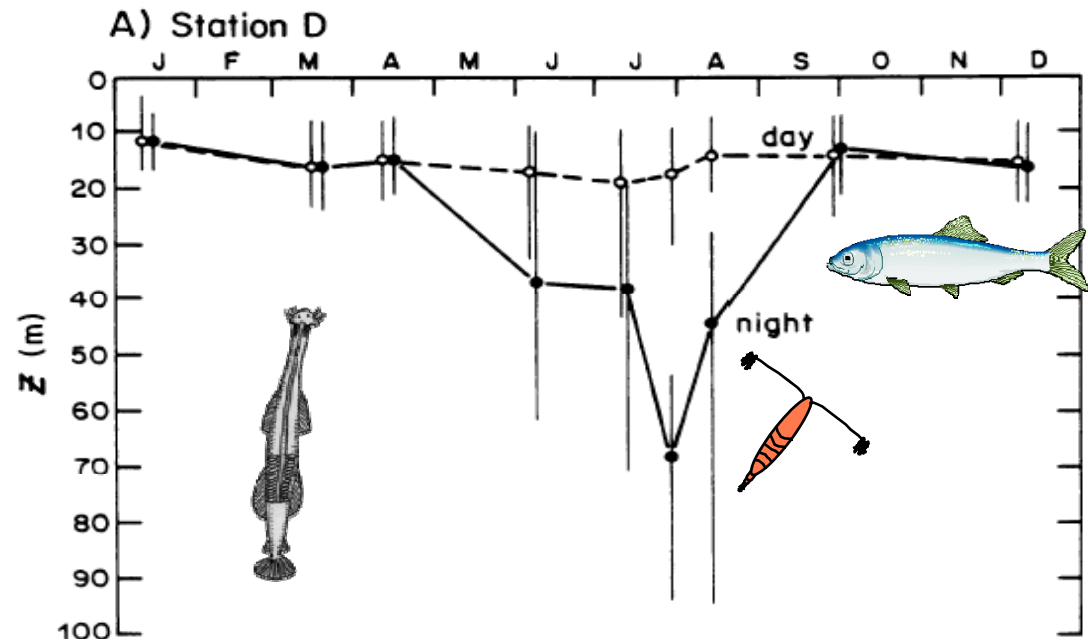
# Fish can structure plankton communities



Brooks & Dodson 1965

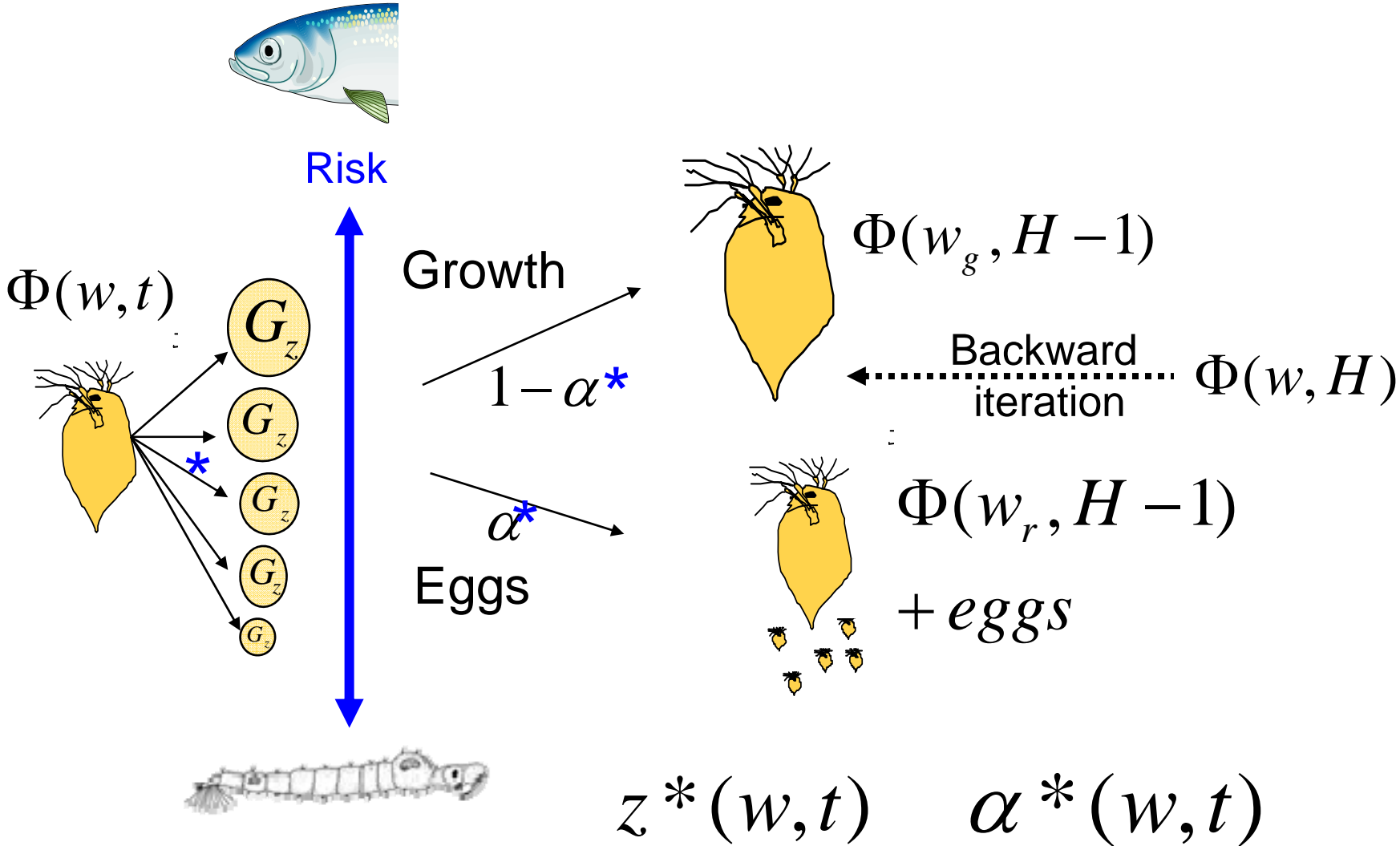


# Plastic behaviour – also in marine zooplankton



Ohman 1990

# Optimal habitat selection and allocation of energy by dynamic programming..



# The dynamic programming equation

Maximise fitness = find the behavioural and life history decision that maximises the sum of current and expected future reproduction:

Fitness (size, time)

$$\Phi(w, t) =$$

Survival

Eggs

Future fitness (new state, time)

$$\max_{z, \alpha} P_s(w, z) \{R(w, z, \alpha) + \Phi[w'(z, \alpha), t + 1]\}$$

# The dynamic programming equation for seasonal environments

Maximise fitness = find the behavioural and life history decision that maximises the sum of current and expected future reproduction:

Fitness (size, time)

$$\Phi(w, t) =$$

Survival

Eggs

Egg fitness  
at t+1

Future fitness (new  
state, time)

$$\max_{z, \alpha} P_s(w, z) \{R(w, z, \alpha) \Phi[egg, t + 1] + \Phi[w'(z, \alpha), t + 1]\}$$

# Computer pseudo-code

```
DEFINE TERMINAL FITNESS(STATE,H)
```

```
DO TIME = H-1, 1, -1
```

```
DO STATE = MINSTATE, MAXSTATE  
DO HABITAT = 1,N_HABITATS  
DO ALLOCATION = 1, N_ALLOCATION
```

Loop over time, state, and decisions

```
Find NEW_STATE(HABITAT, ALLOCATION)  
Find REPRODUCTION(HABITAT, ALLOCATION)  
Find SURVIVAL(HABITAT,ALLOCATION)
```

State dynamics (physiology)  
&  
mechanics

```
Find FITNESS=SURVIVAL*[FITNESS(NEW_STATE,T+1) + REPRODUCTION]
```

```
IF(FITNESS>MAX_FITNESS) THEN  
STORE HABITAT*(STATE,TIME)  
STORE ALLOCATION*(STATE,TIME)  
ENDIF
```

Evaluate consequences of actions  
in terms of fitness and store the best

```
ENDDO ALLOCATION  
ENDDO HABITAT  
ENDDO STATE  
ENDDO TIME
```



Photo: Malin Daase

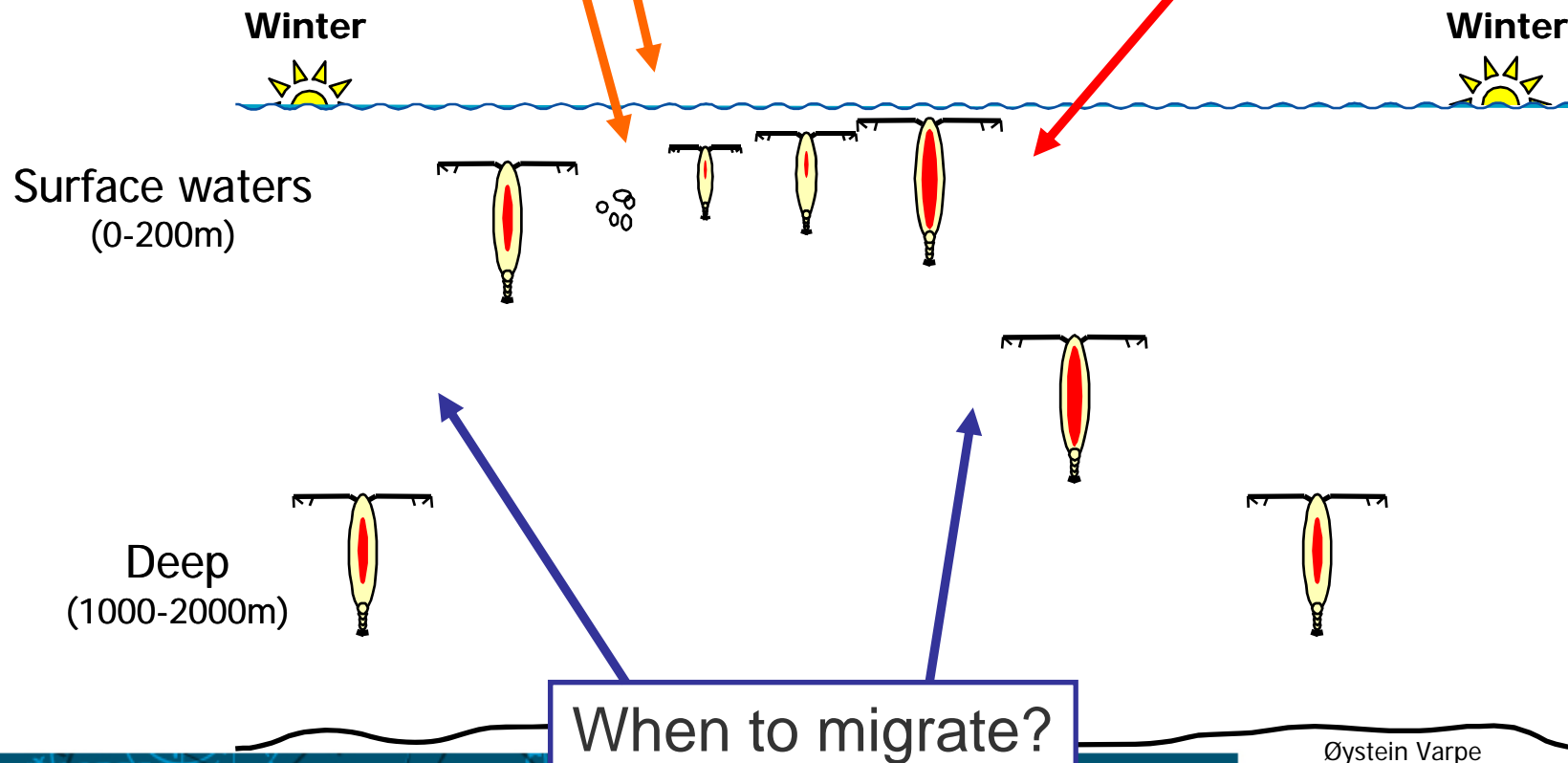
# Seasonal migrations in *Calanus* – the annual routine

When to reproduce?

Capital or income breeding?



How much lipids?



When to migrate?

Øystein Varpe

# Optimal Life History by Dynamic Programming

Fitness of an optimal individual at time t

$$V(x, y, z, t) = \max_{\alpha, \varepsilon, \sigma} \left\{ P_s(y, z, t) \cdot \left[ V(x_{t+1}, y_{t+1}, z_{t+1}, t+1 | \alpha, \varepsilon, \sigma) + b(G, y, \varepsilon) \cdot V_{young}(1, t+1) \right] \right\}$$

Survival probability

Fecundity

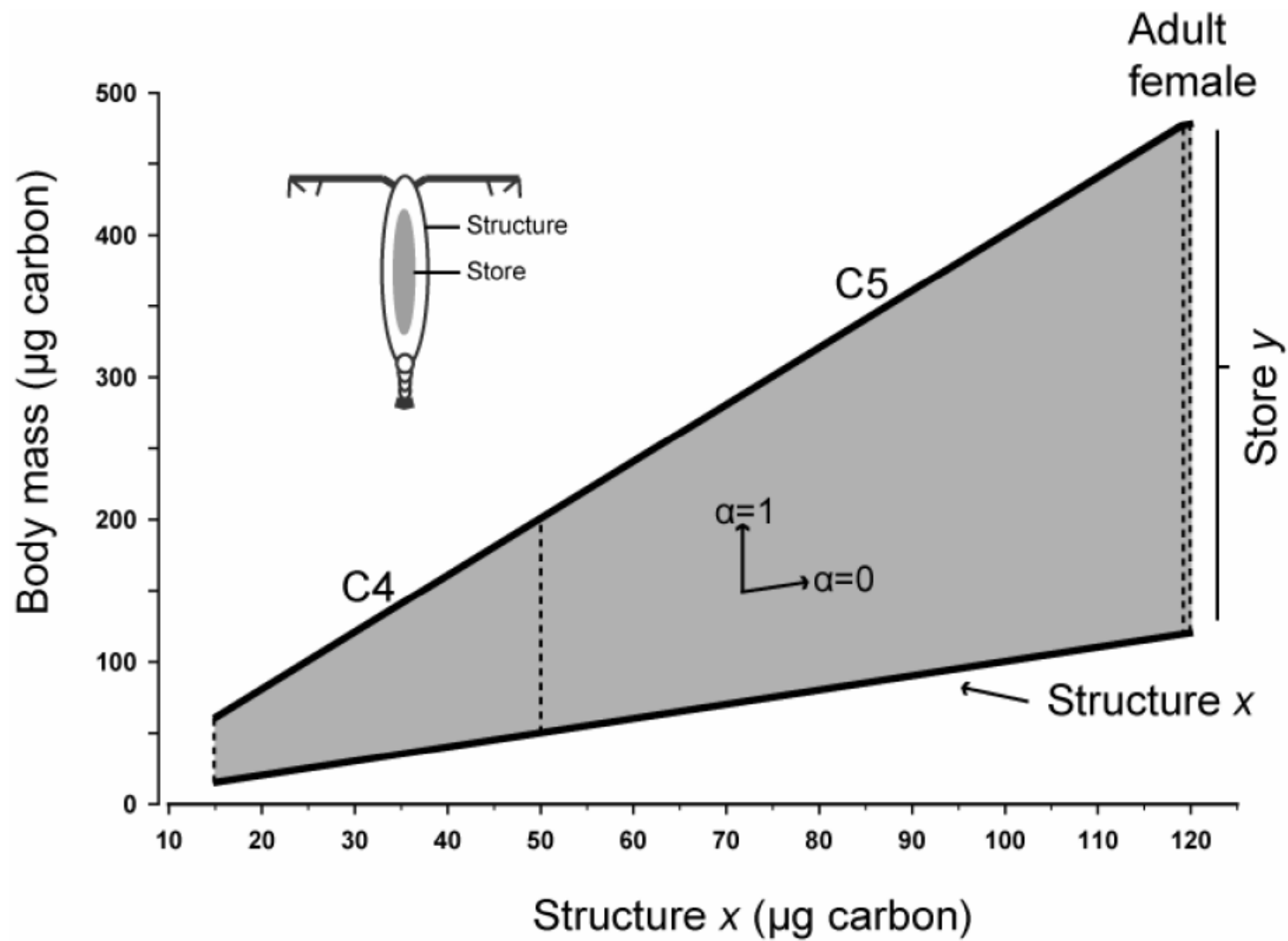
$R_0$  – fitness of an egg at time t+1

Residual RV given LH-decisions

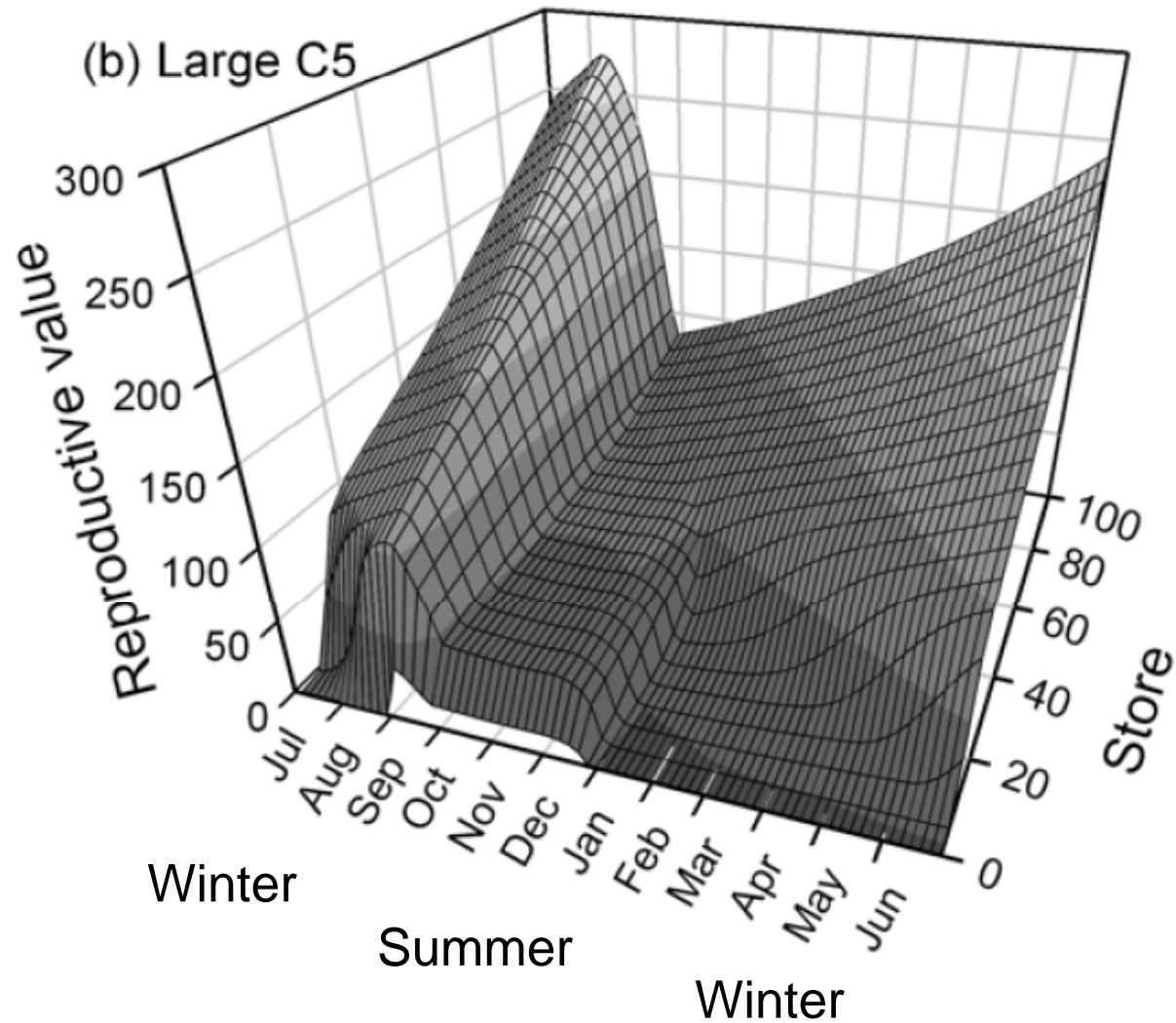
Varpe, Jørgensen, Tarling and Fiksen. (2007). Early is better: seasonal egg fitness and timing of reproduction in a zooplankton life-history model. *Oikos* 116:1331-1342.



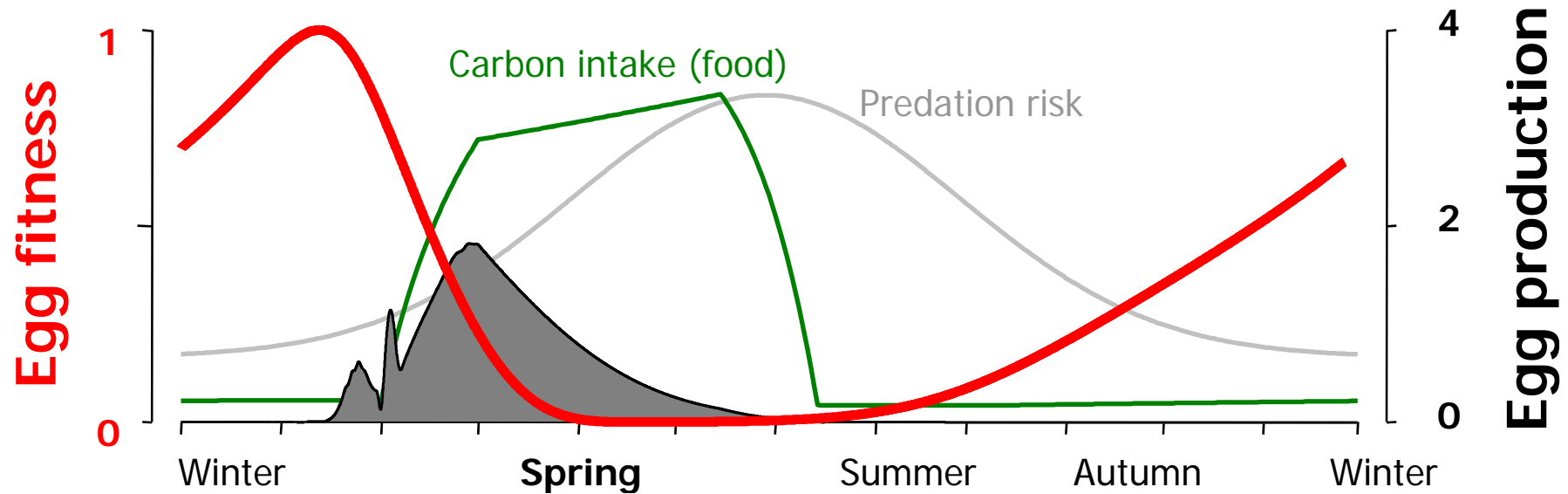
# Energy allocation and state space



# Fitness as a function of state and time

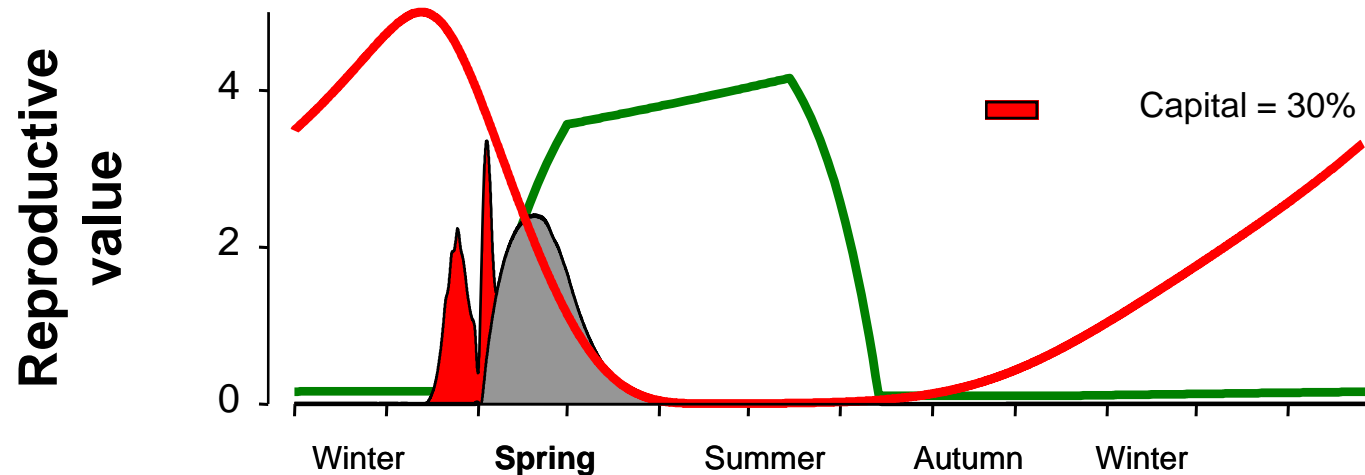
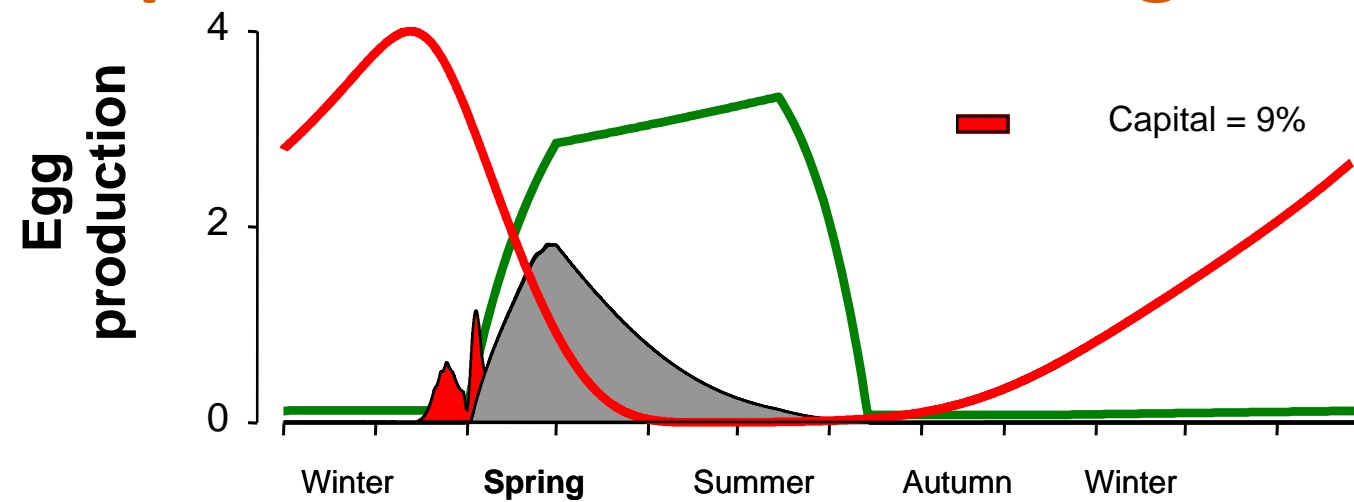


# Egg fitness and population egg production



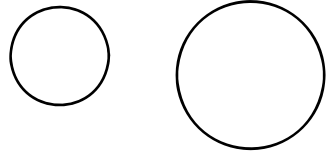
Varpe, Jørgensen, Tarling and Fiksen. (2007). Early is better: seasonal egg fitness and timing of reproduction in a zooplankton life-history model. *Oikos* 116:1331-1342.

# Capital and income breeding

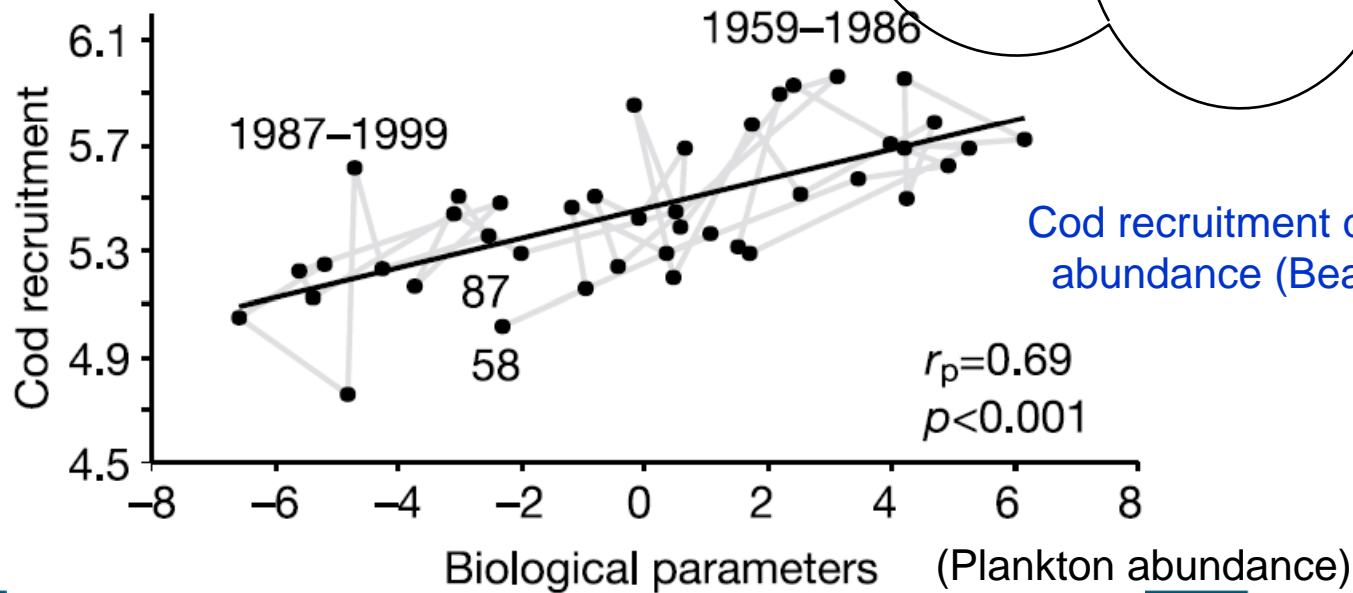
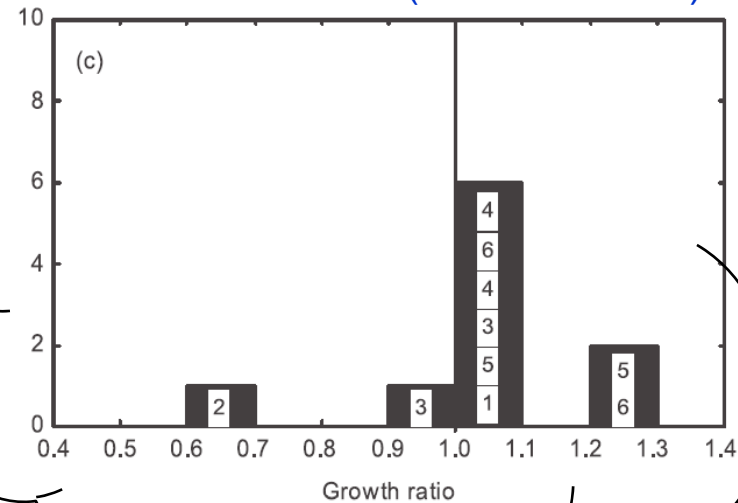


Ø Varpe, C Jørgensen, G. A. Tarling and Ø. Fiksen. (2009). The adaptive value of capital breeding in seasonal environments. *Oikos* 118: 363-370.

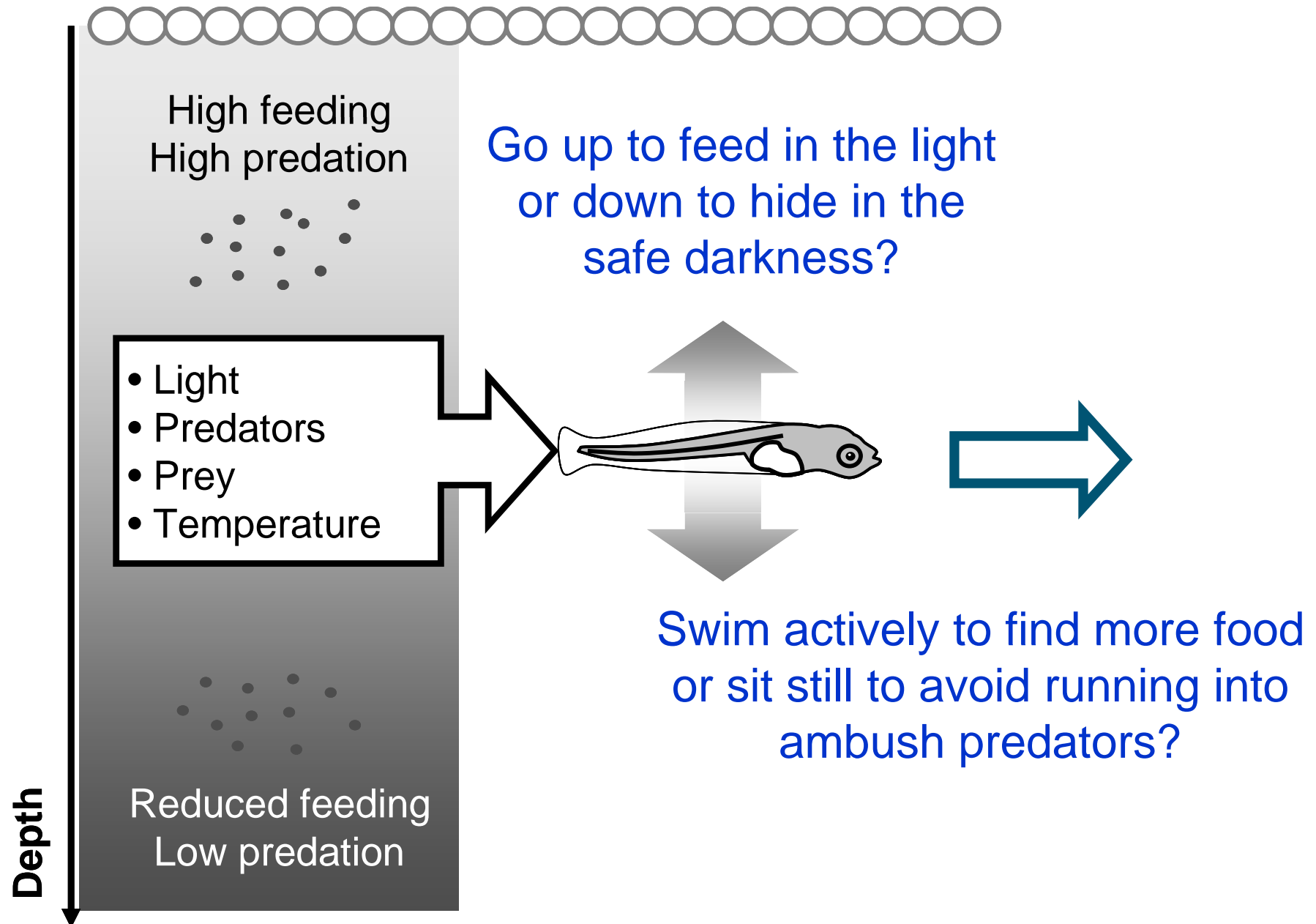
# Larval behaviour and an apparent contradiction



Larval cod tend to grow at maximum rates in the field (Folkvord 2005)

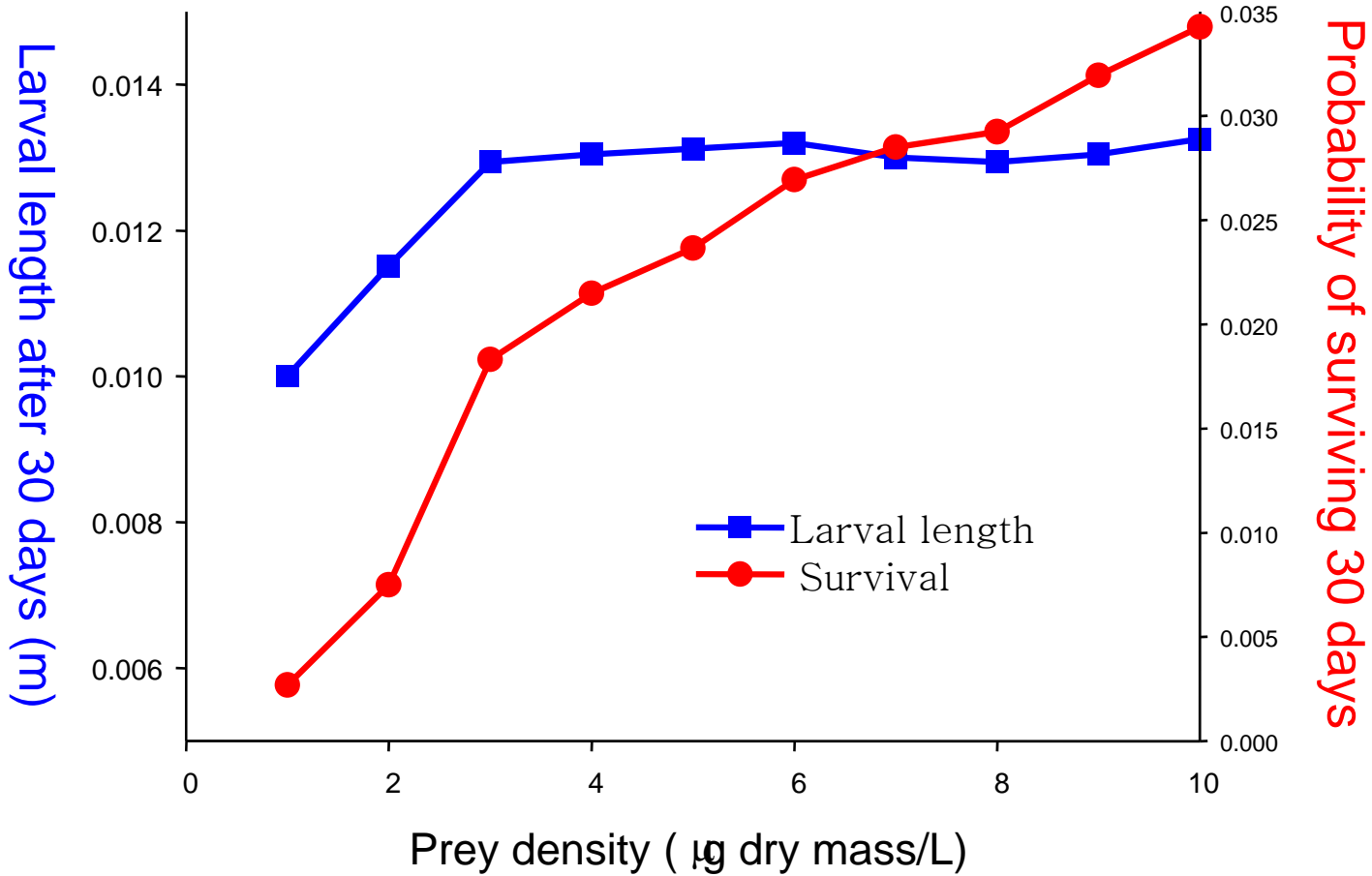


Cod recruitment depends on plankton abundance (Beaugrand & al. 2003)

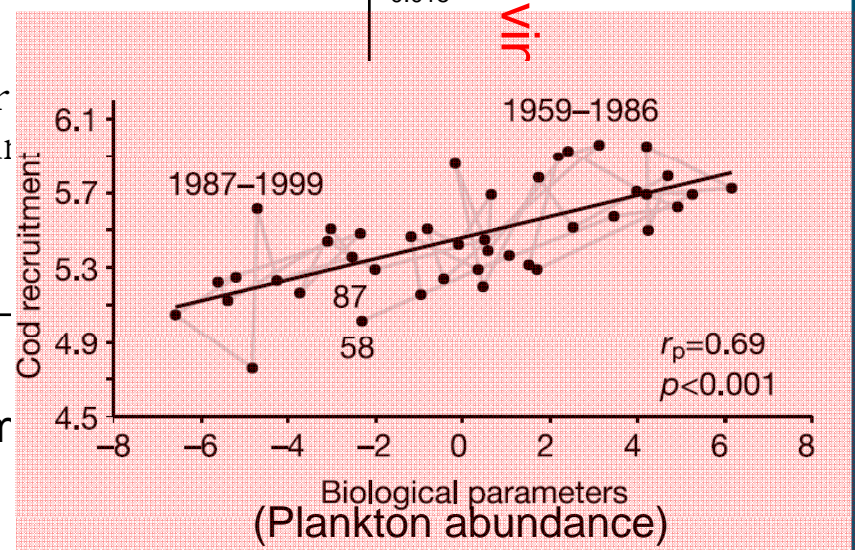
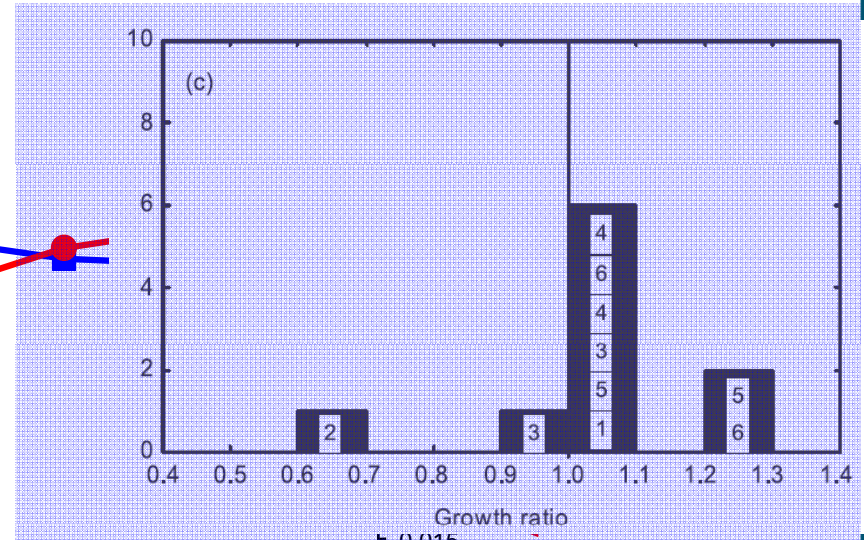
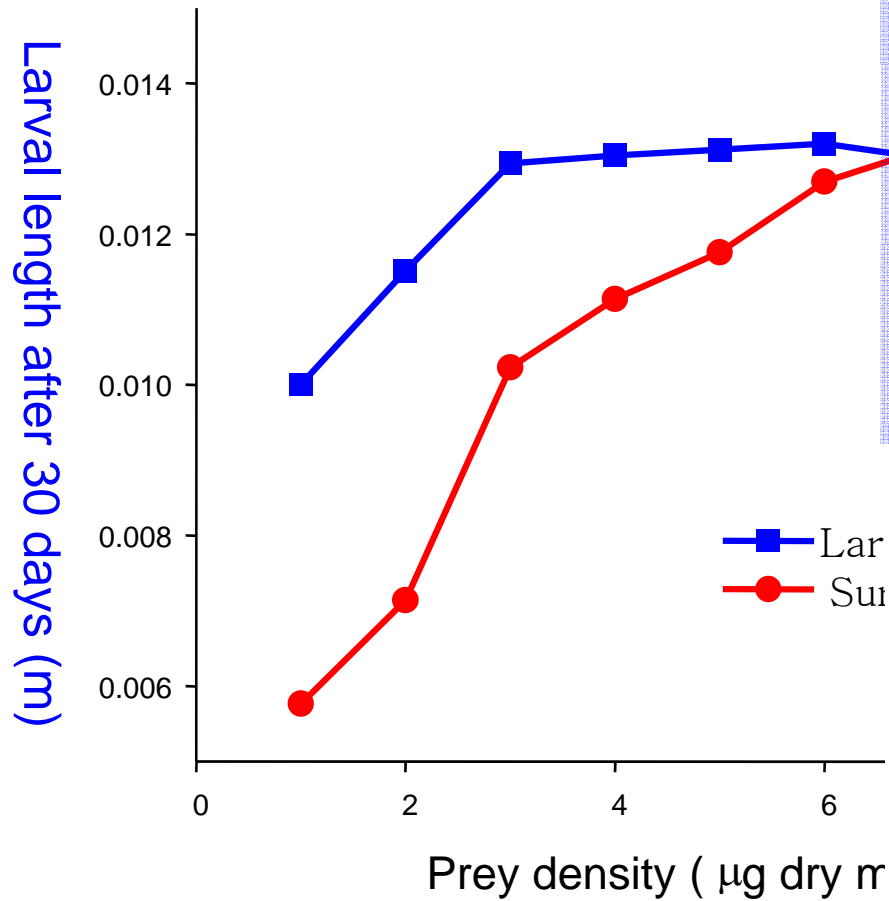


Ø Fiksen and C Jørgensen (2011). Model of optimal behaviour in fish larvae predicts that food availability determines survival, but not growth. *MEPS*. 432:207-219.

# Prey density and recruitment success



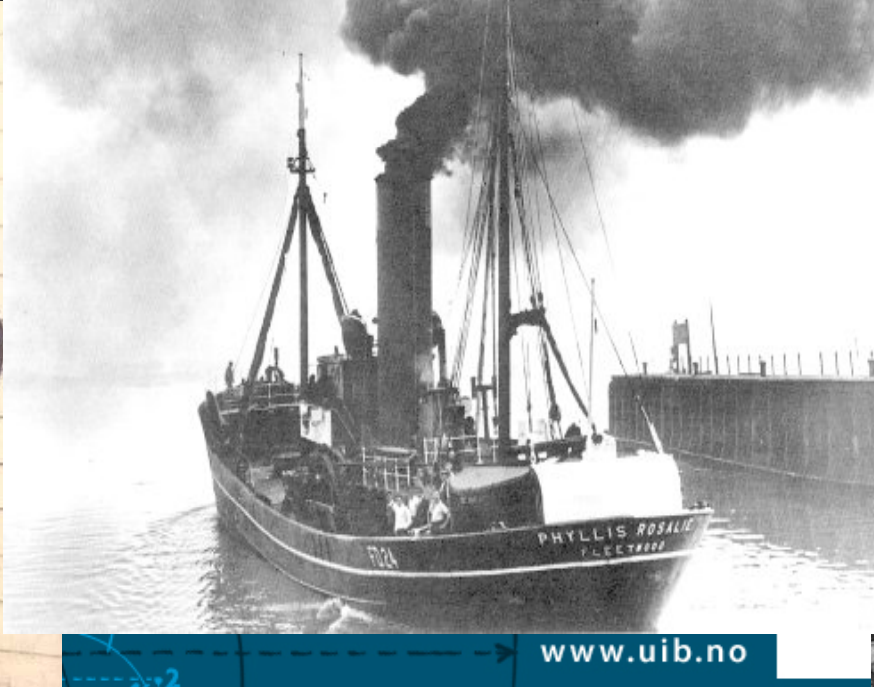
# Prey density and recruitment success



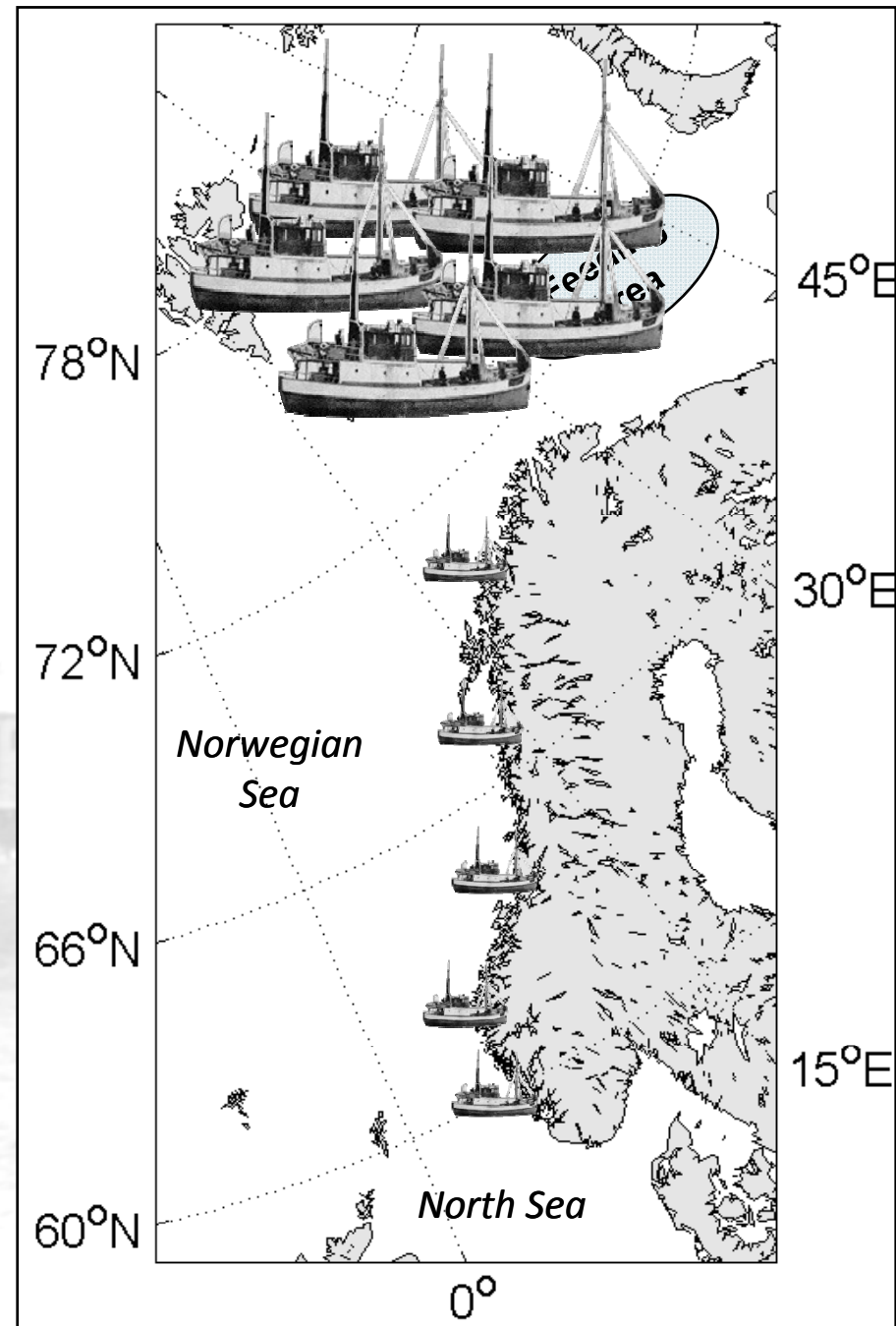




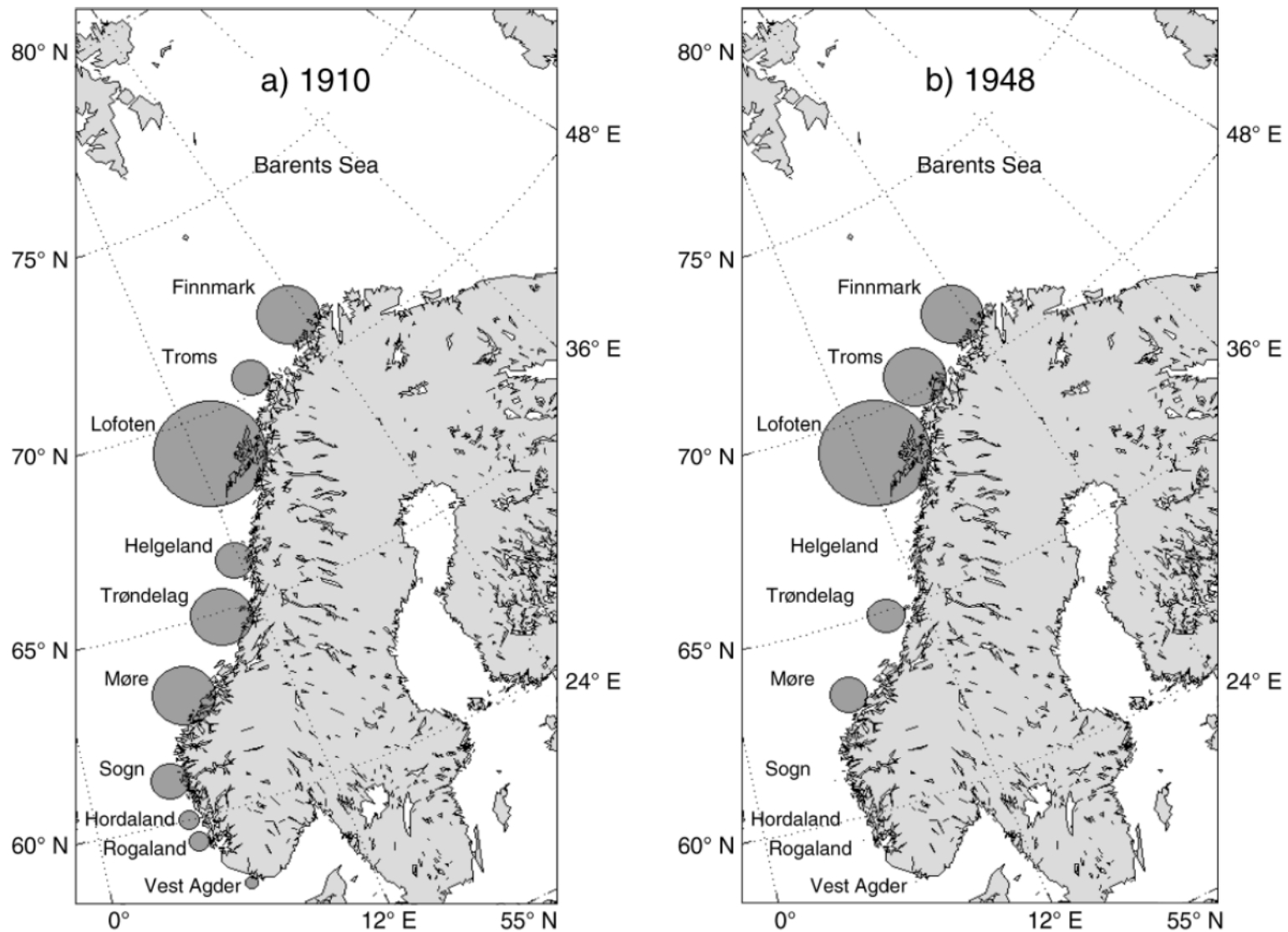
1915  
S. J. ...



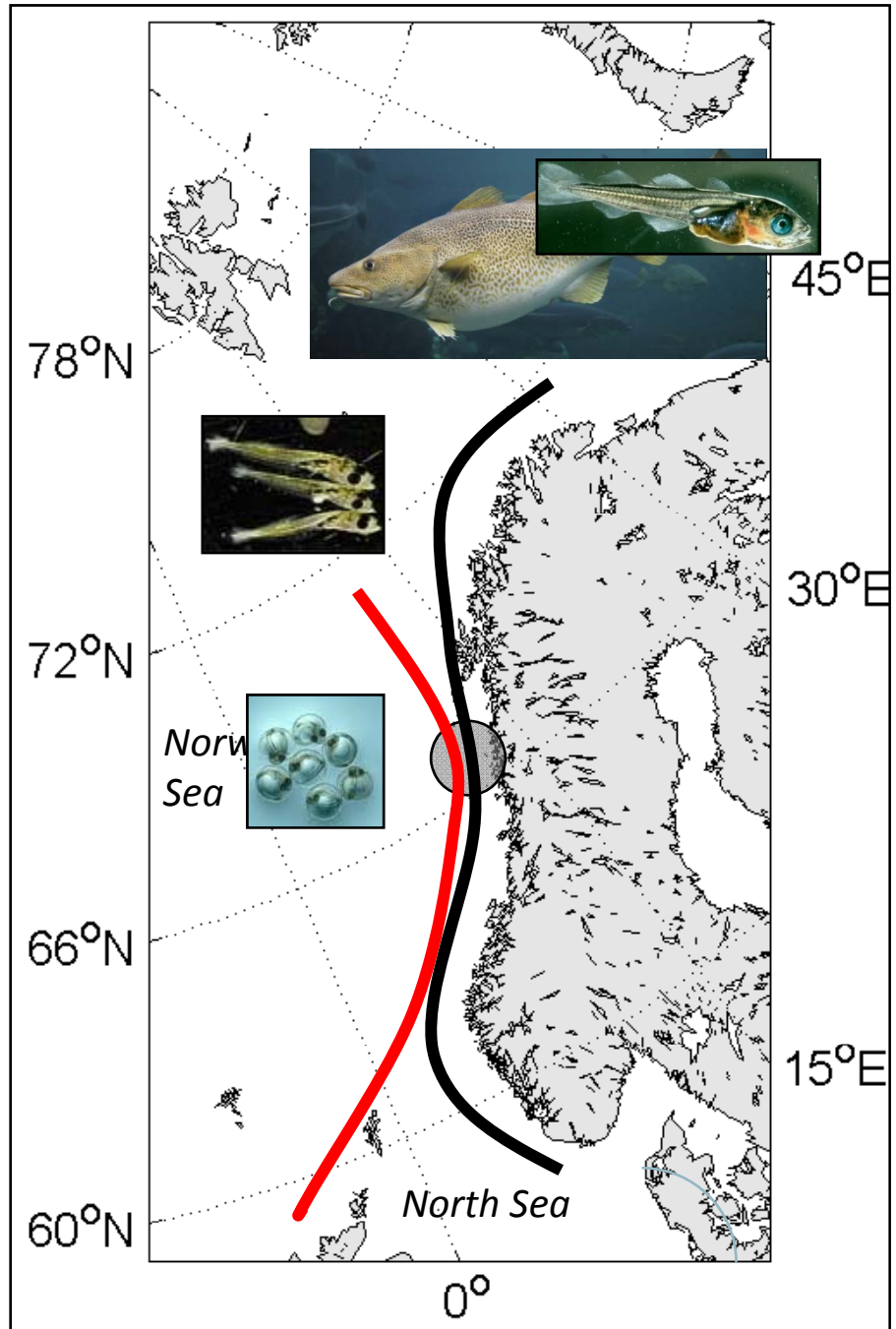
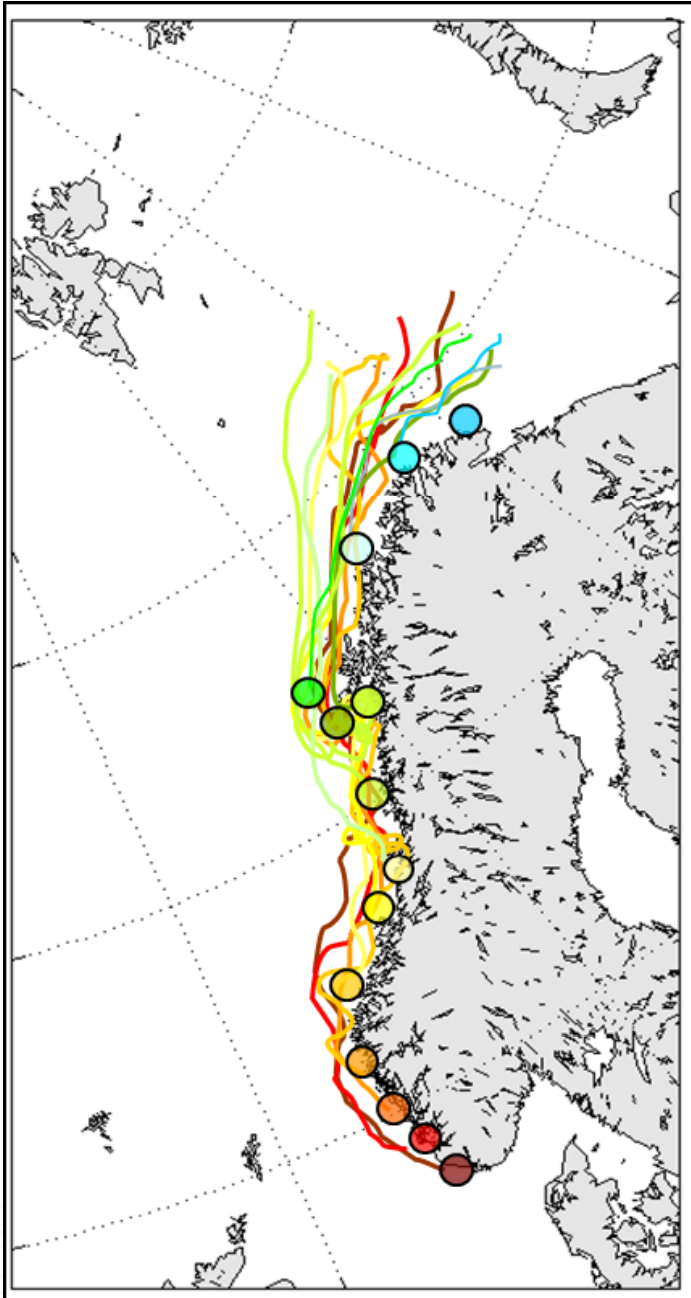
- Before the 1920s, fishing was conducted at the spawning grounds
- In the early 1920s, trawl-fishing started in the Barents Sea
- Fishing intensity in the Barents Sea increased rapidly within a few years



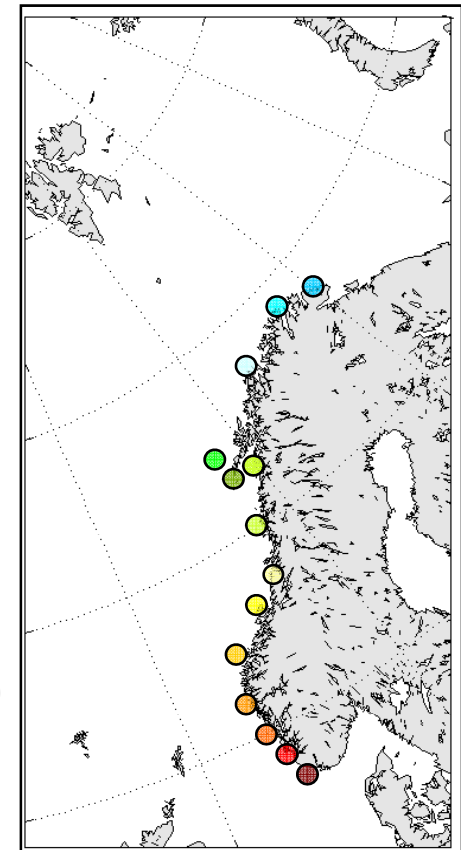
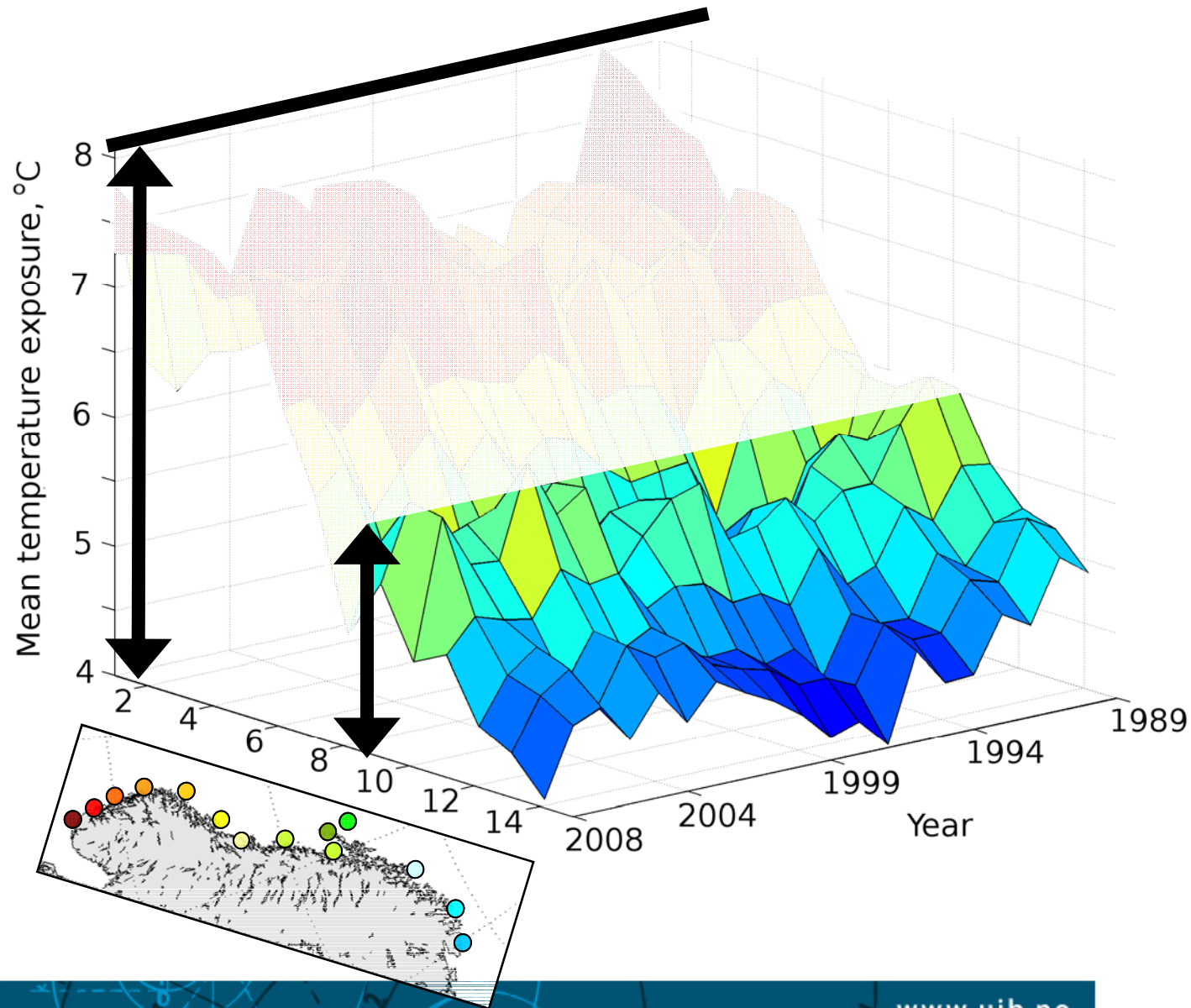
# Historic spawning distributions



Jørgensen C, Dunlop ES, Opdal AF, Fiksen Ø. 2008. *Ecology* **89**:3436-3448.



# Larval temperature exposure



Fitness  
per  
offspring

3

2

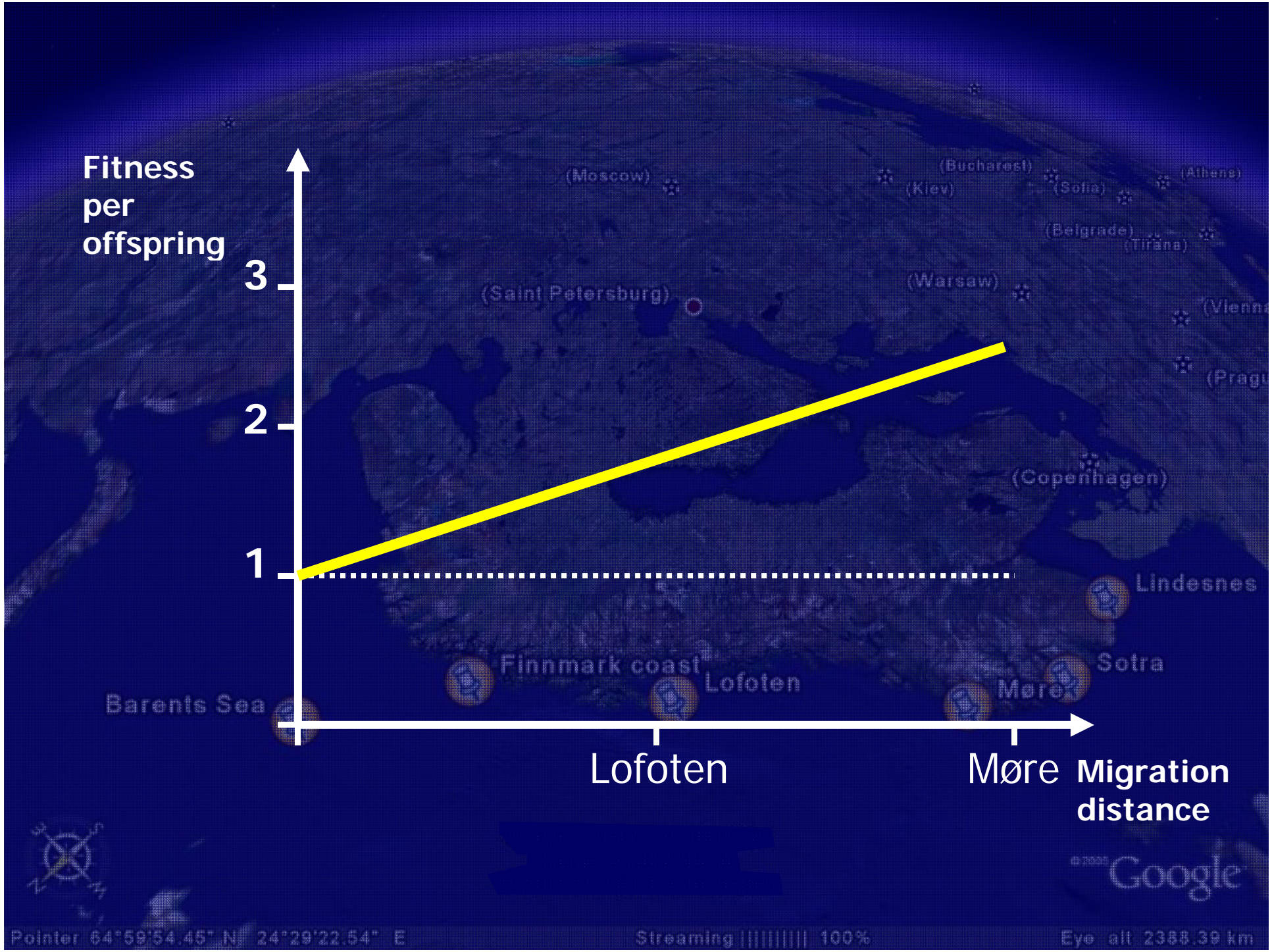
1

Lofoten

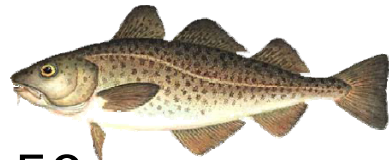
Møre Migration  
distance



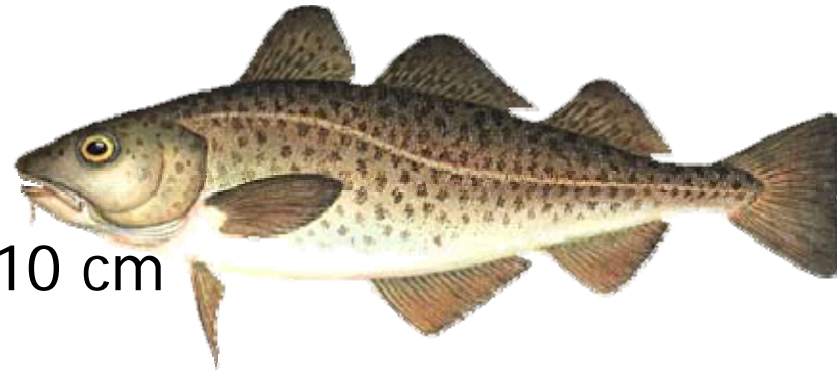
© 2005 Google



# Migration costs versus body size



50 cm

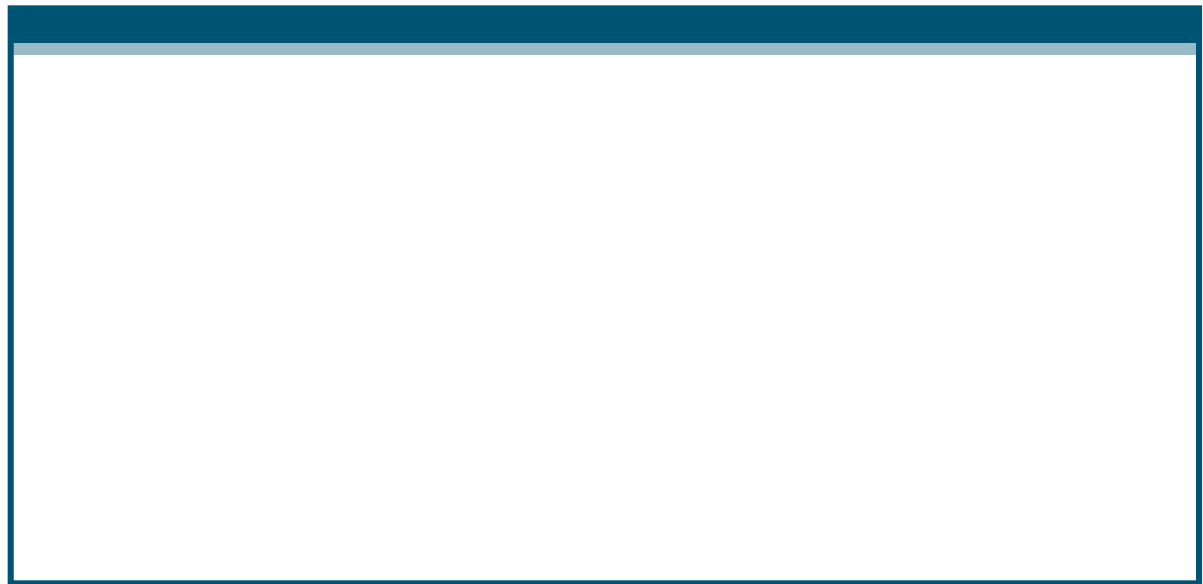


110 cm

Migration S

Migration N

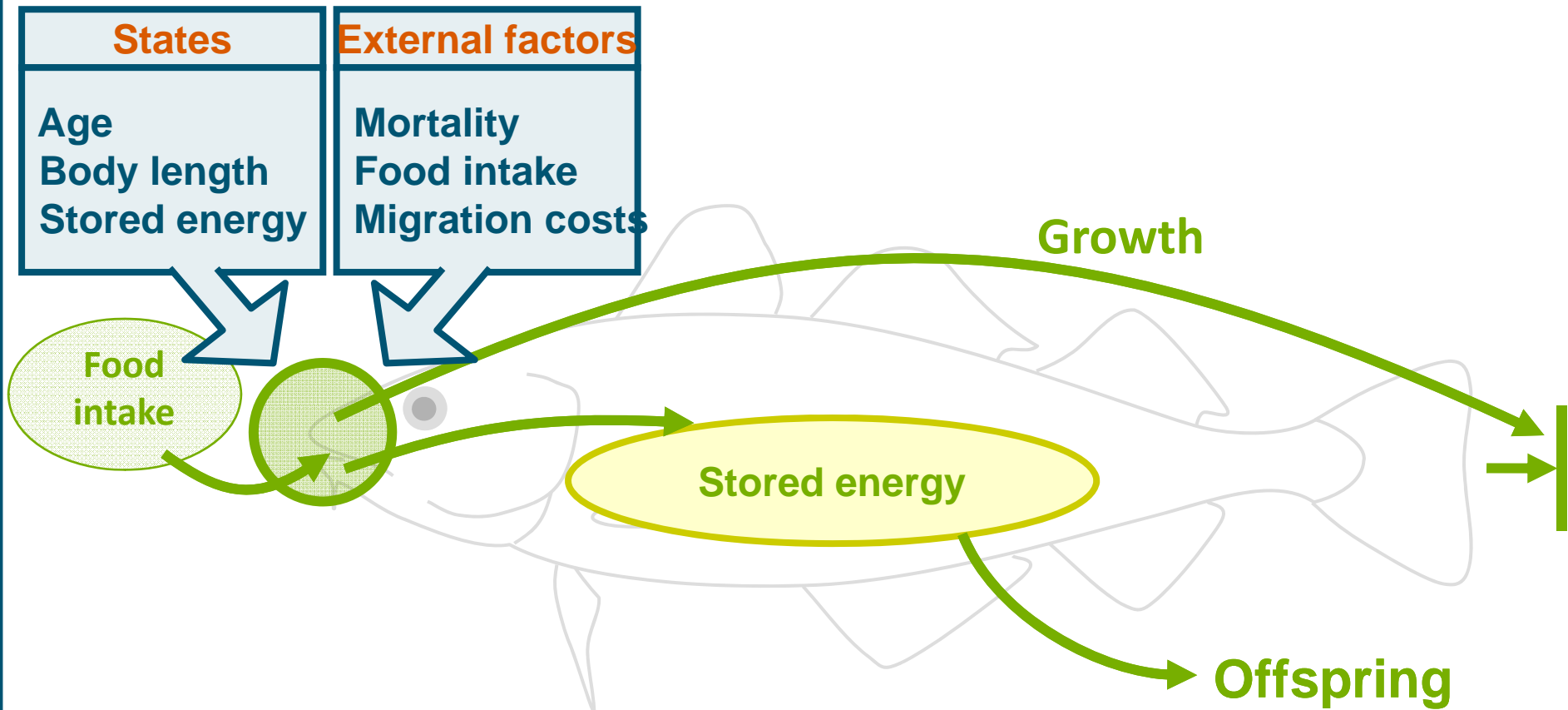
Fecundity



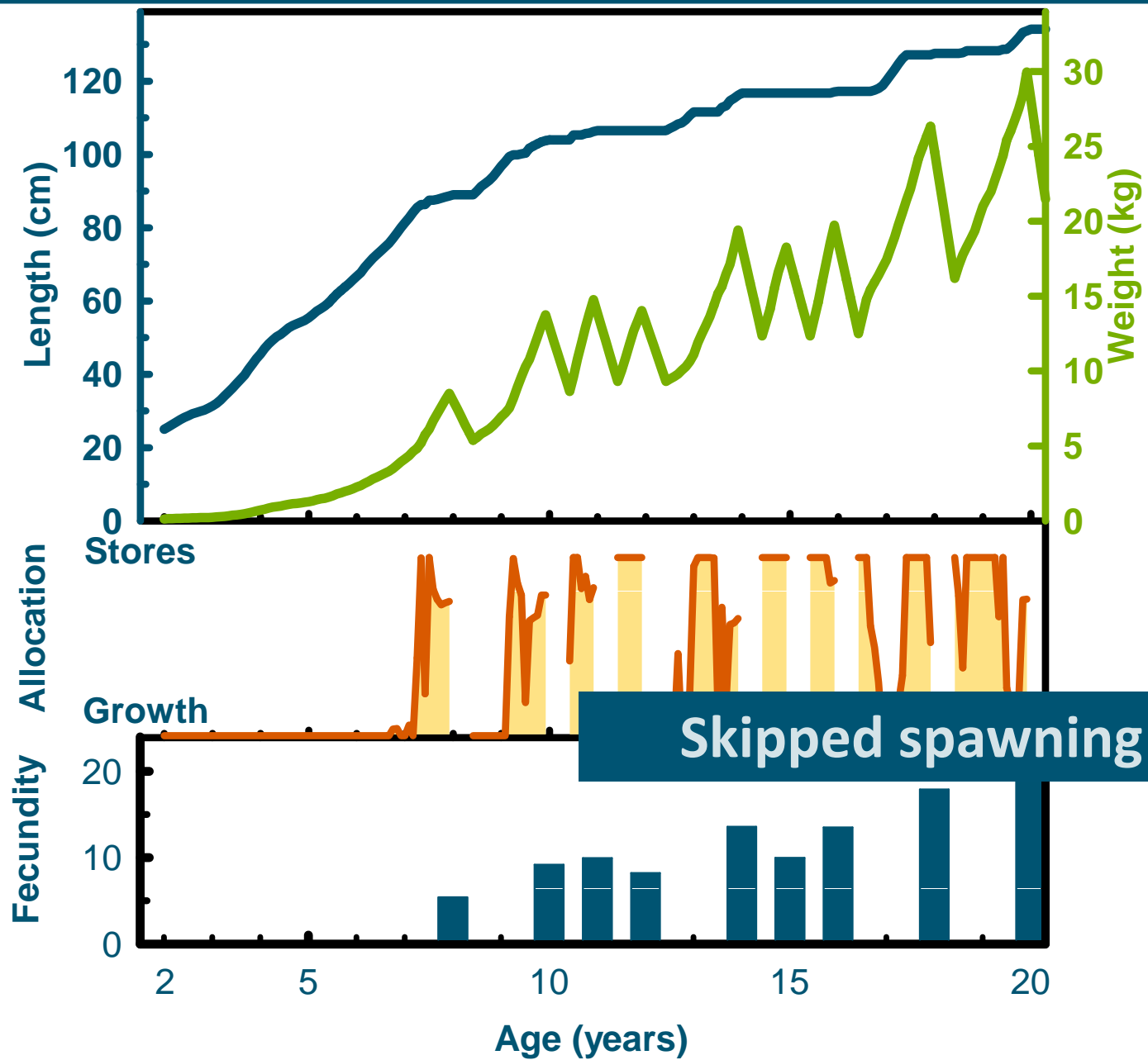
Jørgensen C, Dunlop ES, Opdal AF, Fiksen Ø. 2008. The evolution of spawning migrations: the role of individual state, population structure, and fishing-induced changes. *Ecology* **89**:3436-3448.



# Energy allocation in cod



$$V(A, L, E, F) = \max_{\alpha} \left[ B(E) + S \sum_{F'} P(F' | F) \cdot V(A+1, L', E', F') \right]$$



Jørgensen C and Fiksen Ø. 2006. *Can J Fish Aquat Sci.* **63**:186-199

# Frequent skipped spawning in the world's largest cod population

Jon Egil Skjæraasen<sup>a,b,1</sup>, Richard D. M. Nash<sup>b</sup>, Knut Korsbrekke<sup>b</sup>, Merete Fonn<sup>b</sup>, Trygve Nilsen<sup>c</sup>, James Kennedy<sup>d</sup>, Kjell H. Nedreaas<sup>b</sup>, Anders Thorsen<sup>b</sup>, Peter R. Witthames<sup>e</sup>, Audrey J. Geffen<sup>a</sup>, Hans Høie<sup>a</sup>, and Olav Sigurd Kjesbu<sup>b</sup>

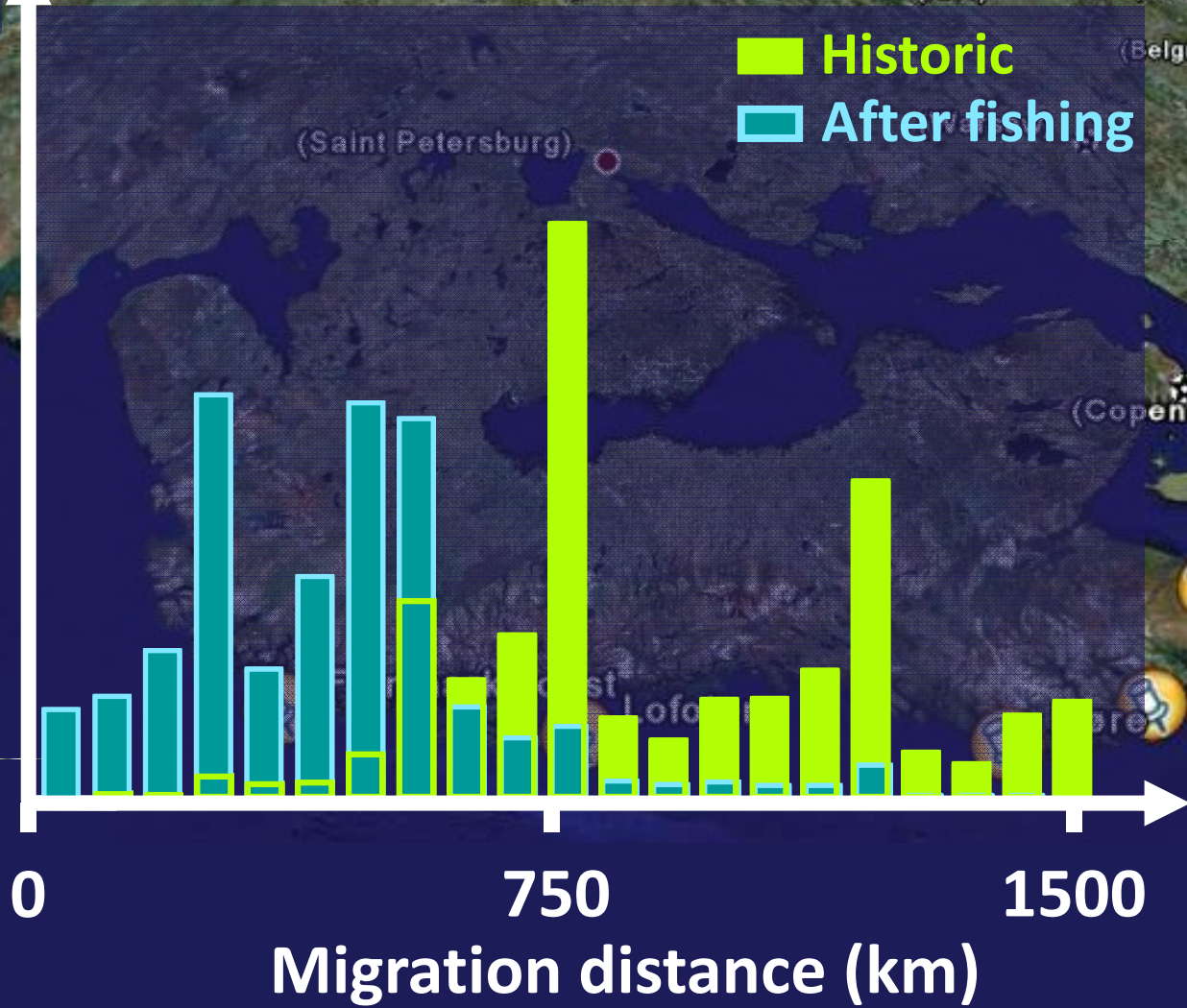
Departments of <sup>a</sup>Biology and <sup>c</sup>Mathematics, University of Bergen, N-5020 Bergen, Norway; <sup>b</sup>Institute of Marine Research, N-5817 Bergen, Norway; <sup>d</sup>Møreforskning Ålesund, N-5021 Ålesund, Norway; and <sup>e</sup>Centre for Environment, Fisheries and Aquaculture Science, Lowestoft, Suffolk NR33 0HT, England

Edited by Ray Hilborn, University of Washington, Seattle, WA, and accepted by the Editorial Board April 16, 2012 (received for review January 5, 2012)

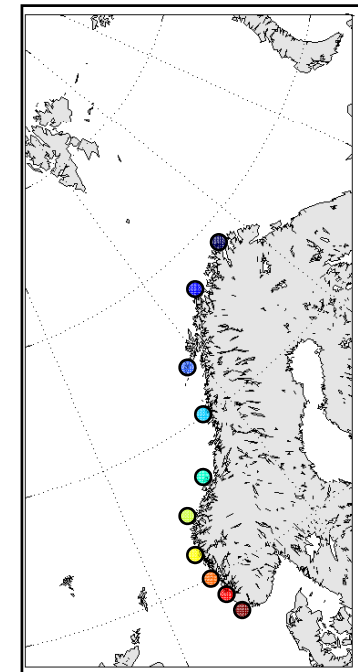
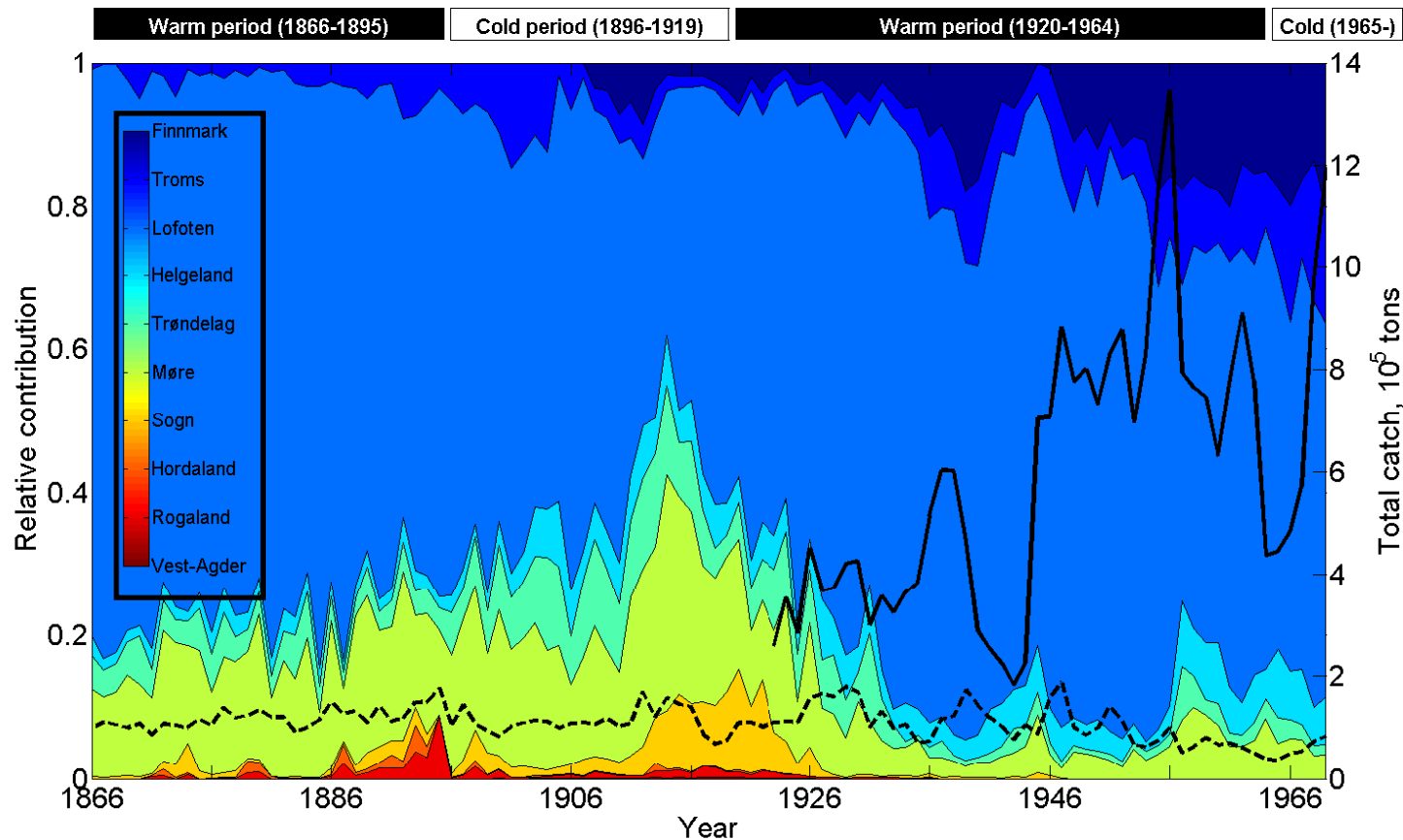
**Life-history theory suggests that animals may skip reproductive events after initial maturation to maximize lifetime fitness. In**

**oocytes are hydrated and the eggs spawned (11). After spawning, the gonad shrinks rapidly in size, visually appearing immature,**

Spawning



# Relative distribution on spawning grounds



## 'NORGES FISKERIER' (1866-1974)

OPDAL AF (2010) Fisheries change spawning ground distribution of northeast Arctic cod.

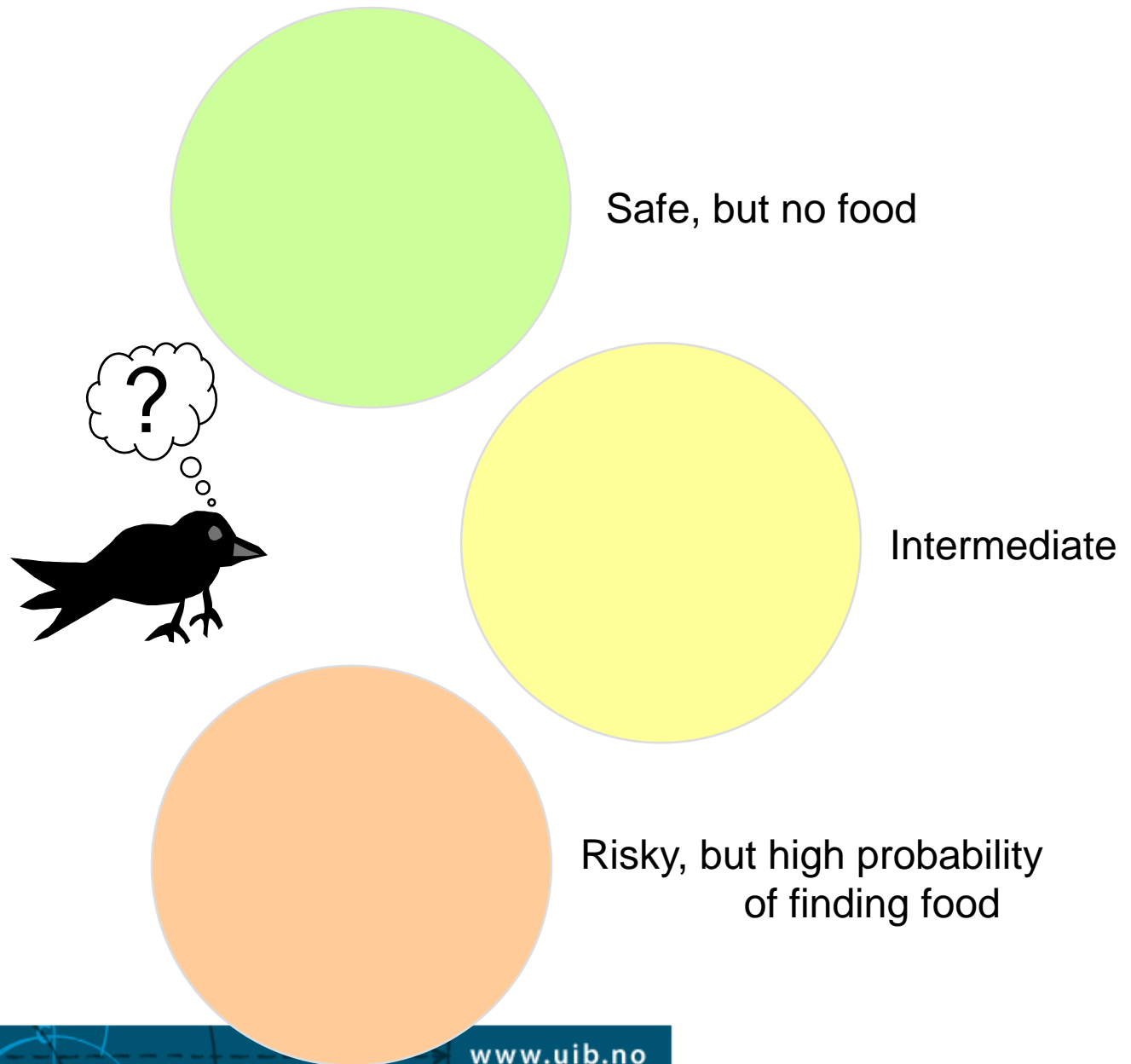
Biol Lett

# Summary

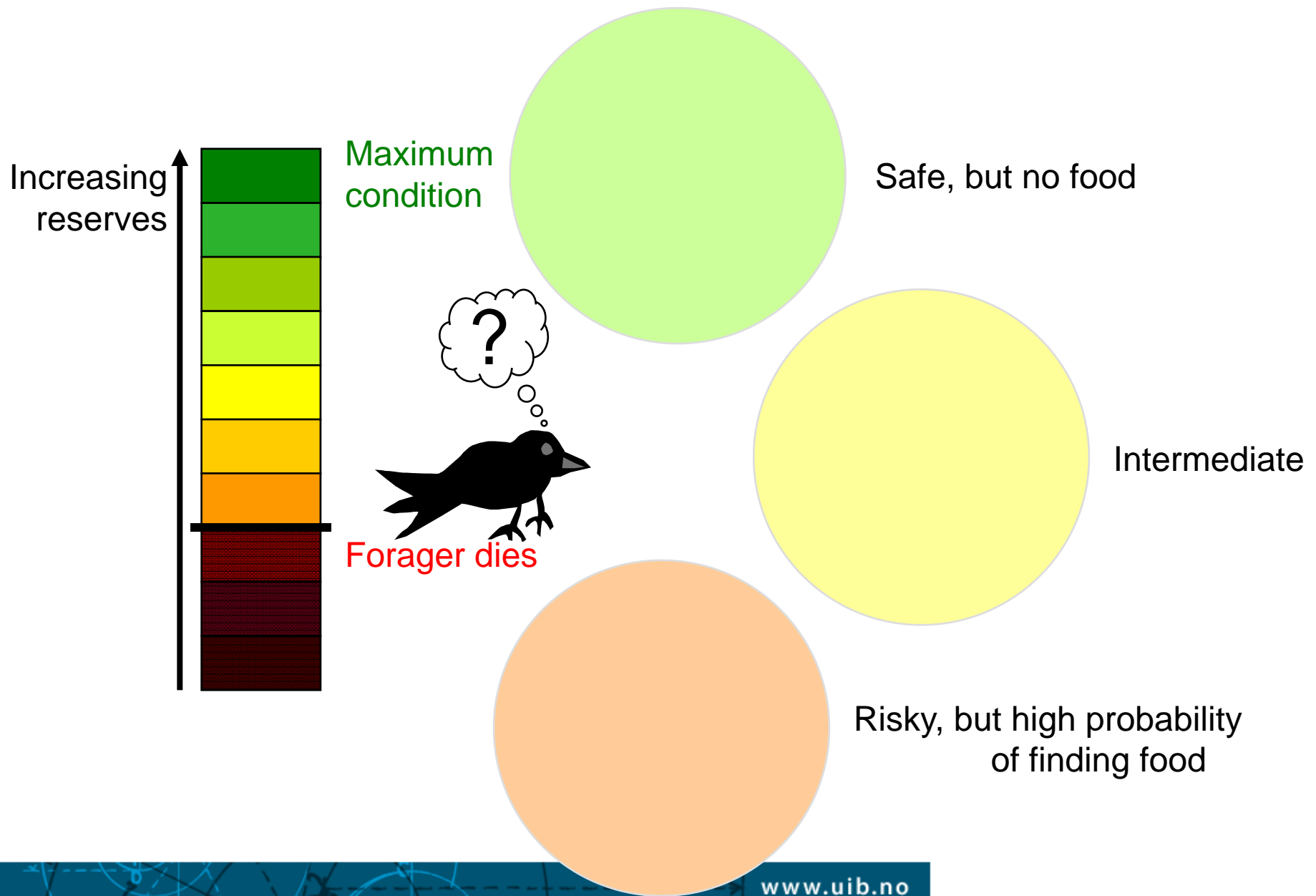
- Dynamic programming is excellent in clarifying the role of state in behavioural ecology and life history theory
- It is integrating proximate constraints, physiology, ecological mechanics and physics with evolutionary theory
- It often surprises you
- It is not suitable for density- or frequency-dependent traits

[www.bio.uib.no/modelling](http://www.bio.uib.no/modelling)

# Optimal patch choice and 'ecology of fear'

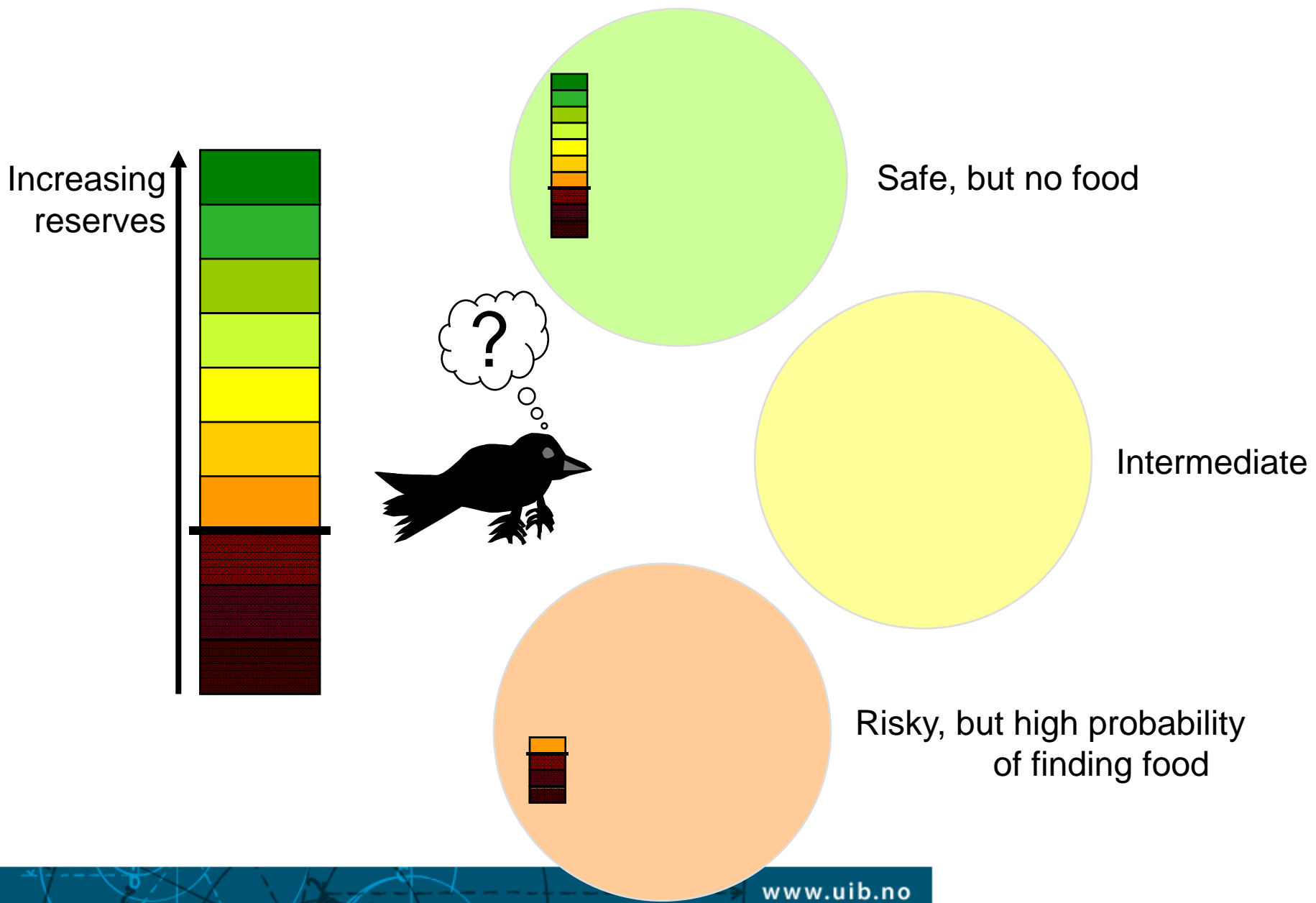


# Individual state: energy reserves





# Individual state influences patch choice



# The model

$X(t)$	State at time $t$ . Constraint: $X(t) < C$
$F(x, t, T)$	Fitness defined as: survival from $t$ until $T$ of an ind in state $X(t) = x$ .
$\alpha_i$	Cost of staying in patch $i$
$\lambda_i$	Probability of finding food in patch $i$
$Y_i$	Value of food in patch $i$ if found
$X_c$	Critical state value – forager dies
$\beta_i$	Predation probability in patch $i$

State change:

$$X(t+1) = \begin{cases} X(t) - \alpha_i + Y_i & \text{with probability } \lambda_i \\ X(t) - \alpha_i & \text{with probability } (1 - \lambda_i) \end{cases} \quad x = \begin{cases} x' \\ x'' \end{cases}$$

Survival    Food is found    No food

$$F(x, t, T) = \max_i (1 - \beta_i) \cdot [ \lambda_i \cdot F(x', t+1, T) + (1 - \lambda_i) \cdot F(x'', t+1, T) ]$$

## A model: parameters

	Safe, but no food	Inter- mediate	Risky, with food
	Patch 1	Patch 2	Patch 3
Cost of choosing patch $i$ , $\alpha_i$	1	1	1
Predation probability, $\beta_i$	0.000	0.004	0.020
Probability of finding food, $\lambda_i$	0.0	0.4	0.6
State increment if food is found, $Y_i$	0	3	5
Expected return, $\lambda_i \cdot Y_i$	0.0	1.2	3.0

$$F(x, t, T) = \max_i (1 - \beta_i) \cdot [ \lambda_i \cdot F(x', t+1, T) + (1 - \lambda_i) \cdot F(x'', t+1, T) ]$$